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*Algorithms for the Lusternik-Schnirelmann category of finite topological spaces.*

Topological complexity (TC) is a homotopy invariant rooted in the robot motion planning problem. Given a path-connected space  $X$  that represents a robot's space of configurations,  $TC(X)$  gives the minimum number of continuous motion planning rules required to program that robot to move from one position into another position. It is not unreasonable to assume a robot is only capable of obtaining finitely many positions. When the space is  $T_0$ , we can model that finite space by a poset,  $P$ . In an absence of algorithms for directly computing the TC, there has been interest in the upper- and lower-bounds of TC. A popular bound is determined by the Lusternik-Schnirelmann category, which is the minimal number of open sets covering a space whose inclusion is nullhomotopic. For a finite space  $P$ , this yields the upper-bound

$$TC(P) \leq cat(P)^2.$$

In this talk, we present original theorems and algorithms used in determining  $cat(P)$ , including a Python class in which we have implemented these results. (Received September 15, 2020)