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Kohji Yanagawa* (yanagawa@kansai-u.ac.jp). *When is a Specht ideal Cohen-Macaulay?* Preliminary report.

Let $R = K[x_1, \dots, x_n]$ be a polynomial ring over a field K of characteristic 0, and λ a partition of n . For a Young tableau T with shape λ , we have its *Specht polynomial* $f_T(x) \in R$. The symmetric group S_n acts on the K -vector space U_λ spanned by $\{f_T(x) \mid T \text{ is a Young tableau with shape } \lambda\}$. An S_n -module U_λ is called a *Specht module*, and U_λ 's give a complete list of irreducible representations of S_n .

So let us consider the *ideal* $I_\lambda^{\text{Sp}} := (U_\lambda) \subset R$. If R/I_λ^{Sp} is CM, then λ is of the form either $(a, 1, \dots, 1)$, (a, b) , or $(a, a, 1)$. First, $R/I_{(a,1,\dots,1)}^{\text{Sp}}$ can be seen as a determinantal ring, and is CM (a joint work with Junzo Watanabe). If $\lambda = (a, b)$ or $(a, a, 1)$, then we have

$$\sqrt{I_\lambda^{\text{Sp}}} = \bigcap_{F \subset \{1, \dots, n\}, \#F=a+1} (x_i - x_j \mid i, j \in F).$$

A result of Etingof et al. states that $R/\sqrt{I_\lambda^{\text{Sp}}}$ is CM *in these cases*. Our main result is the following.

Theorem. $R/I_{(a,b)}^{\text{Sp}}$ is reduced, and hence CM.

The case $\lambda = (a, a, 1)$, $a \geq 5$ is open. (Received January 19, 2019)