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**Jim Hoste\***, jhoste@pitzer.edu, and **Patrick D. Shanahan**. *A  $\mathbb{Z} \oplus \mathbb{Z}$ -family of knot quandles*. Preliminary report.

Suppose  $K$  is an oriented knot in a 3-manifold  $M^3$  with regular neighborhood  $N(K)$ . For each element  $\gamma \in \pi_1(\partial N(K))$  we define a quandle  $Q_\gamma(K; M^3)$  which generalizes the concept of the fundamental quandle of a knot. In particular, when  $\gamma$  is the meridian of  $K$ , we obtain the fundamental quandle. The collection of all such quandles gives a  $\mathbb{Z} \oplus \mathbb{Z}$ -family of quandles. If  $K$  is a knot in  $M$  and  $\gamma$  is a primitive element, then we show that there exists a knot  $K'$  in a 3-manifold  $M'$  such that  $Q_\gamma(K; M) \cong Q_\mu(K'; M')$  where  $\mu$  is the meridian of  $K'$ . Starting with a partially framed link  $L$  in  $S^3$  where the framed components give a surgery description of the manifold  $M$  and a single unframed component represents  $K$  we can derive a similar surgery description of  $K'$  in  $M'$ . Using results of Fenn and Rourke, we may then use this description of  $K'$  to record a presentation of the quandle  $Q_\gamma(K; M)$ . We describe a number of examples of these quandles for knots in various manifolds. (Received January 28, 2019)