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**Shehzad Ahmed\*** (sa066513@ohio.edu), Ohio University, Department of Mathematics 321  
Morton Hall, Athens, OH 45701. *The Weak pcf Conjecture.*

Recall that, for a set  $A$  of regular cardinals, we define

$$\text{pcf}(A) := \{\text{cf}(\prod A/D) : D \text{ is an ultrafilter on } A\}.$$

In the case that  $A$  is an interval of regular cardinals satisfying  $|A| < \min(A)$ , we know that  $|\text{pcf}(A)| < |A|^{+4}$ . This bound allows us to show that, for example, if  $\aleph_\omega$  is a strong limit singular cardinal, then  $2^{\aleph_\omega} < \aleph_{\omega_4}$ . In the event that  $A$  is not an interval of regular cardinals, we know of no such bound on  $|\text{pcf}(A)|$ . A conjecture of Shelah's is that, if  $A$  is a set of regular cardinals with  $|A| < \min(A)$ , then  $\text{pcf}(A)$  has no inaccessible accumulation point. In this talk, I will discuss why this is an important conjecture, and discuss some of its consequences. (Received August 20, 2018)