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Simon Bortz, Steve Hofmann, Jose Luis Luna* (j1lwwc@mail.missouri.edu), **Svitlana Mayboroda** and **Bruno Poggi**. *Solvability of Elliptic Equations with Lower Order Terms*.

The study of boundary value problems for second order elliptic equations of the form

$$-\operatorname{div}A\nabla u = 0 \quad \text{in } \mathbb{R}_+^{n+1}, \quad (1)$$

for an elliptic matrix A , has a long and celebrated history. In this talk we will focus on generalizing well-posedness of the standard Boundary Value Problems (Dirichlet, Neumann and Regularity) to equations with lower order terms of the form

$$-\operatorname{div}(A\nabla u + B_1 u) + B_2 \cdot \nabla u + V u = 0, \quad \text{in } \mathbb{R}_+^{n+1}. \quad (2)$$

Here we will assume the lower order terms lie in the critical spaces

$$B_i \in L^n(\mathbb{R}^n; \mathbb{C}^{n+1}), \quad V \in L^{n/2}(\mathbb{R}^n),$$

with $\|B_i\|_{L^n(\mathbb{R}^n)}$, $\|V\|_{L^{n/2}(\mathbb{R}^n)}$ small. Finally we will require that all the coefficients in (??) are independent of the vertical variable.

Our results state roughly that, under the above hypotheses on the lower order terms, the well-posedness (suitably defined) in $L^2(\partial\mathbb{R}_+^{n+1})$ for (??) is inherited from the corresponding property for the equation (??).

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