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Alex J Feingold* (alex@math.binghamton.edu), Dept of Math Sciences, Whitney Hall, Binghamton University, 4400 Vestal Parkway East, Binghamton, NY 13902-6000. *Hyperbolic Kac-Moody algebras and groups*. Preliminary report.

Several approaches to the study of hyperbolic Kac-Moody (KM) algebras, \mathfrak{g} , and their groups, G , will be discussed. (1) New insights of Carbone-Feingold-Freynd come from the embedding of the twin building for G in the union of Tits cones in the real compact form of \mathfrak{g} . (2) New work with Kleinschmidt-Nicolai concerns imaginary root groups in hyperbolic KM groups. (3) Decomposition of \mathfrak{g} with respect to a subalgebra \mathfrak{k} provides information about the structure of \mathfrak{g} using the representation theory of \mathfrak{k} . Feingold-Frenkel (1983) studied the rank 3 hyperbolic \mathfrak{g} with Weyl group $PGL(2, \mathbb{Z})$ and affine \mathfrak{k} of type $A_1^{(1)}$. That \mathfrak{g} contains all rank 2 hyperbolic KM algebras with symmetric Cartan matrices (Feingold-Nicolai 2004). The case when \mathfrak{k} is the rank 2 “Fibonacci” hyperbolic was studied in Penta’s 2016 dissertation. In addition to \mathfrak{k} itself and infinitely many irreducible highest and lowest weight \mathfrak{k} -modules, Penta found four other integrable \mathfrak{k} -modules in the decomposition of \mathfrak{g} which are neither highest nor lowest weight modules. Weight multiplicity formulas for these “non-standard” modules are not yet known, but a recursive algorithm for computing a basis provided numerical data suggestive of a Racah-Speiser type multiplicity formula. (Received January 16, 2020)