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**Monica Lewis\*** (malewi@umich.edu). *The local cohomology of a parameter ideal with respect to an arbitrary ideal.*

Let  $R$  be a regular ring, let  $J$  be an ideal generated by a regular sequence of codimension at least 2, and let  $I$  be an ideal containing  $J$ . We give an example of a module  $H_I^3(J)$  with infinitely many associated primes, answering a question of Hochster and Núñez-Betancourt in the negative. In fact, for  $i \leq 4$ , we show that under suitable hypotheses on  $R/J$ ,  $\text{Ass } H_I^i(J)$  is finite if and only if  $\text{Ass } H_I^{i-1}(R/J)$  is finite. Our proof of this statement involves a novel generalization of an isomorphism of Hellus, which may be of some independent interest. The finiteness comparison between  $\text{Ass } H_I^i(J)$  and  $\text{Ass } H_I^{i-1}(R/J)$  tends to improve as our hypotheses on  $R/J$  become more restrictive. To illustrate the extreme end of this phenomenon, at least in the prime characteristic  $p > 0$  setting, we show that if  $R/J$  is regular, then  $\text{Ass } H_I^i(J)$  is finite for all  $i \geq 0$ . (Received August 08, 2020)