Heba Ayeda, David Beecher, Xiaoxiao Cui* (xiaoxiaocui@cpp.edu), Alan Krinik, Jeremy Lin, Thuy Vu Dieu Lu, David Perez, Randall J. Swift and Weizhong Wong. Gambler's ruin probabilities for finite birth-death chains with alternating probabilities and the ballot box problem for couples.

<u>PROBLEM 1</u>. Consider a finite birth-death chain on states: 0, 1, 2, ..., H - 1, H having absorbing states at 0 and H, alternating ascending probabilities, alternating descending probabilities and alternating return probabilities at states 1, 2, 3, ..., H - 1. Then for each state i, 0 < i < H and for each $n \in \mathbb{N}$, we determine the exact *n*-step ruin (transition) probability $P^{(n)}(i, 0)$ in terms of explicit eigenvalue expressions. This result follows from duality theory and eigenvalue results for tridiagonal matrices having alternating entries (Kouachi, S. 2008). <u>PROBLEM 2</u>. The traditional two candidate Ballot Box Problem is extended to include *couple* voters. This model assumes the relevant transition matrices to be symmetric, penta-diagonal, Toeplitz and sub-stochastic. The closed form solution of this problem is obtained in terms of explicit eigenvalue expressions for transition matrices of size 8X8 or less. (Received September 21, 2021)