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# Index

We generally indicate the first occurrence only. The data include the typical notation (if any), the serial number of the definition, theorem, etc. explaining the notion or denomination, and finally the page number in parentheses.

D2.1.6 means Definition 2.1.6, and letters T, L, E instead of D refer to the theorem, lemma, and exercise with the given number. P1.3.3 stands for the proof of Theorem 1.3.3, 4.1.E3 denotes Example 3 in Section 4.1, 5.7 means Section 5.7, and A.7/2 refers to Subsection 2 in Section A.7.

We add a sign “–” or “+” to the number of definition, theorem, etc., if the notion is introduced not in the given definition, theorem, etc., but just before or after it, without a new serial number. E.g., DA.10.6+ indicates at the phrase “transcendental number” that it is explained *after* Definition A.10.6.

In some cases, we include an important theorem besides the definition. E.g., for “subspace” we refer both to Definition 4.2.1 and Theorem 4.2.2.

For information about notation used in the book, please consult part “Technical details” in the Introduction. The phrasing of a definition or theorem is closed by a ♣ sign, the end of a proof is denoted by ■. We add that as mentioned in another part of the Introduction, exercises marked with one or two asterisks are considered hard or extra hard by our judgement, and the boldface serial number indicates that a detailed solution can be found at [bookstore.ams.org/amstext-66](http://bookstore.ams.org/amstext-66).

<b>C</b> = complex numbers	3-repetition code, 10.1.E2, (231)
$F$ = generally denotes a field	
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<b>R</b> = real numbers	absolute value of a vector, $\ \mathbf{x}\ $ , D8.2.1, (182)
<b>Z</b> = integers	accompanying transformation, T5.8.1, (127)
$\mathbf{Z}[x]$ = polynomials with integer coefficients	
2-repetition code, 10.1.E1, (231)	

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