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The symbol  $\star$  denotes either a more advanced section, or else a bit of a digression, which can be skipped without interrupting the flow of the rest of the book.

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