
General index

A bold page number points to the page where the term is defined or used in an especially significant way. The number in parentheses is the page number on which the cited exercise may be found.

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