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# Subject index

Page numbers are printed in **boldface** when they represent the definition of, or the main source of information about, the topic being indexed. For brevity, we sometimes use “F.” to denote “Fourier”, “H. I.” for “Hölder Inequality”, “M. I.” for “Minkowski Inequality”, and “trig.” for “trigonometric”.

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