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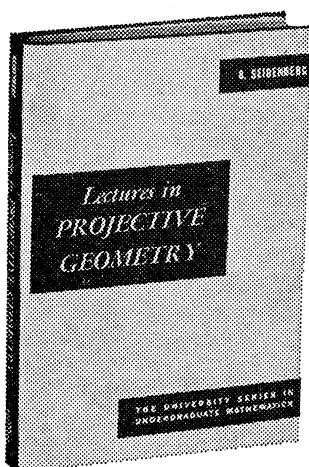
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CONTENTS

March, 1962

Book Reviews

A. Kratzer and W. Franz. <i>Transzendente Funktionen</i> . Reviewed by A. Erdélyi.....	51
H. S. M. Coxeter. <i>Introduction to geometry</i> . Reviewed by H. Freudenthal.....	55
Konrad Jacobs. <i>Neuere Methoden und Ergebnisse der Ergodentheorie</i> . Reviewed by P. R. Halmos.....	59
H.-J. Kowalsky. <i>Topologische Räume</i> . Reviewed by J. R. Isbell	60
John von Neumann. <i>Continuous geometry</i> . Reviewed by Garrett Birkhoff.....	61
The November Meeting in Milwaukee, Wisconsin. By J. W. T. Youngs.....	62
The November Meeting in Gainesville. By G. B. Huff.....	63
The November Meeting in Santa Barbara. By R. S. Pierce.....	64
Report of the Treasurer. By A. E. Meder, Jr.....	65
Research Problems.....	68

Research Announcements

N. G. de Bruijn and H. S. Wilf. On Hilbert's inequality in n dimensions.....	70
Katsumi Nomizu and Hideki Ozeki. On the degree of differentiability of curves used in the definition of the holonomy group.....	74
P. E. Conner and E. E. Floyd. Differentiable periodic maps	76
Barry Mazur. Simple neighborhoods.....	87
R. A. Kunze. On the irreducibility of certain multiplier representations.....	93
Gian-Carlo Rota. An "Alternierende Verfahren" for general positive operators.....	95
Louis de Branges. Entire functions and integral transforms..	103
C. C. Chang and H. J. Keisler. Model theories with truth values in a uniform space.....	107
A. Kosinski. Singularities of piecewise linear mappings. I. Mappings into the real line.....	110
D. L. Hanson. On the representation problem for stationary stochastic processes with trivial tail field.....	115
F. B. Jones. On the existence of a small connected open set with a connected boundary.....	117
L. Carlitz. Some theorems on permutation polynomials....	120
Teng-sun Liu. On vanishing algebras.....	123