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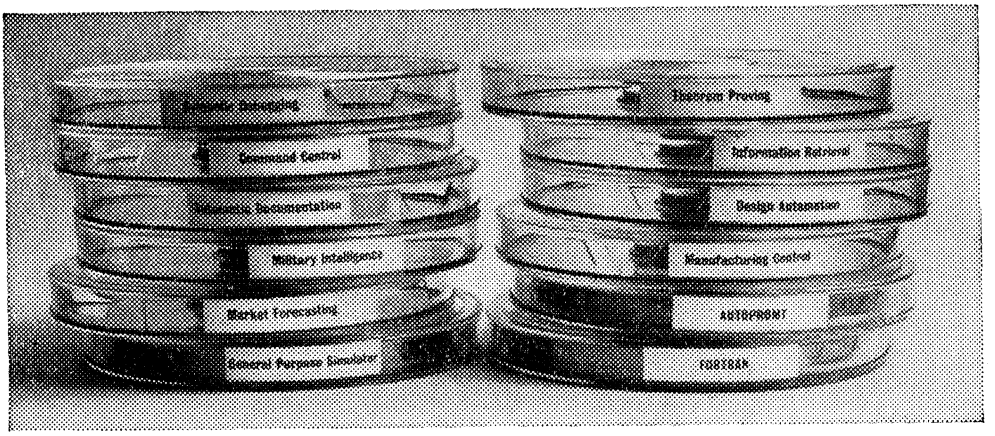

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TABLE OF CONTENTS
July 1962

Some Relations and Values for the Generalized Riemann Zeta Function ..... *Eldon R. Hansen and Merrell L. Patrick*

Euler's Constant to 1271 Places ..... *Donald E. Knuth*

A Calculation of the Number of Lattice Points in the Circle and Sphere ..... *W. Fraser and C. C. Gotlieb*

Sign Wave Analysis in Matrix Eigenvalue Problems ..... *K. M. Brown and P. Henrici*

Acceleration Techniques for Iterated Vector and Matrix Problems .... *P. Wynn*

Computing Error Bounds in Solving Linear Systems ..... *J. Schröder*

A Note on Finite Difference Methods for Solving the Eigenvalue Problems of Second-Order Differential Equations ..... *M. R. Osborne*

A Method for Computing the Circular Coverage Function ..... *A. R. Didonato and M. P. Jarnagin*

Optimum-Point Formulas for Osculatory and Hyperosculatory Interpolation ..... *Herbert E. Salzer*

TECHNICAL NOTES AND SHORT PAPERS

A Heuristic Asymptotic Formula Concerning the Distribution of Prime Numbers ..... *Paul T. Bateman and Roger A. Horn*

Primitive Polynomials (Mod. 2) ..... *E. J. Watson*

Note on Latent Roots and Vectors of Segments of the Hilbert Matrix ..... *H. H. Denman and R. C. W. Ettinger*

Expansions of Jacobian Elliptic Function in Powers of the Modulus .... *Y. K. Lin and F. A. Lee*

A Note on the Curve Fitting of Discrete Data by Economization ..... *F. D. Burgoyne*

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CONTENTS—*Continued from back cover*

Kuo-Tsai Chen. An expansion formula for differential equations 341
V. S. Varadarajan. On a problem in ergodic theory 345
R. V. Chacon. Operator averages 351
Lars Hörmander. Differential operators with nonsingular characteristics 354
C. D. Papakyriakopoulos. A reduction of the Poincaré conjecture to other conjectures 360
S. Helgason. Some results on invariant theory 367
R. M. Blumenthal, R. K. Getoor and H. P. McKean, Jr. Markov processes with identical hitting distributions 372
M. Koecher. On real Jordan algebras 374
Samuel I. Goldberg and Shoshichi Kobayashi. The conformal transformation group of a compact homogeneous Riemannian manifold 378
Gabriel Stolzenberg. Polynomially convex sets 382
John Stallings. Groups with infinite products 388
H. E. Rauch. The singularities of the modulus space 390
Raoul Bott. A note on the KO-theory of sphere-bundles 395
G. T. Cargo. A connection between Tauberian theorems and normal functions 400
Takayuki Tamura. Certain characterization of singular semigroups 402
J. R. Rice. Tchebycheff approximation in a compact metric space 405
K. de Leeuw and H. Mirkil. Algebras of differentiable functions 411
W. A. J. Luxemburg. Two applications of the method of construction by ultrapowers to analysis 416
A. Erdélyi. Singular perturbations 420
H. Bass and S. Schanuel. The homotopy theory of projective modules 425
H. D. Block and W. H. J. Fuchs. Acknowledgment 428

CONTENTS

July, 1962

J. J. Stoker. Some observations on continuum mechanics with emphasis on elasticity 239
Charles B. Morrey, Jr. Some recent developments in the theory of partial differential equations 279
John Wermer. Uniform approximation and maximal ideal spaces .. 298
Research Problem 305

Book Reviews

A. M. OSTROWSKI, Solution of equations and systems of equations. Reviewed by D. M. Young, Jr. 306
J. G. HOCKING and G. S. YOUNG, Topology. Reviewed by Alex Heller 308
ZEEV NEHARI, Introduction to complex analysis. Reviewed by George Springer 310
A. DINGHAS, Vorlesungen über Funktionentheorie. Reviewed by Maurice Heins 311
DETLEF LAUGWITZ, Differential geometrie. Reviewed by Leon Green 313
The April Meeting in Chicago. By J. W. T. Youngs 315
The April Meeting in Atlantic City. By J. W. Green and Everett Pitcher 316
The April Meeting in Monterey. By R. S. Pierce 319

Research Announcements

Joseph Lewittes. Invariant quadratic differentials 320
J. A. Nohel. Some problems in nonlinear Volterra integral equations 323
L. Sucheston. A zero-one property of mixing sequences of events 330
François Treves. The equation $(\partial^2/\partial x^2+\partial^2/\partial y^2+(x^2+y^2)(\partial/\partial t))^2u+\partial^2u/\partial t^2=f$, with real coefficients, is "without solutions" 332
J. H. Curtiss. Solution of the Dirichlet problem by interpolating harmonic polynomials 333
Shoshichi Kobayashi. Homogeneous Riemannian manifolds of negative curvature 338
Anders Hyllengren. On the quotient of entire functions of lower order less than one 340

Continued on inside back cover

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