# CONTEMPORARY MATHEMATICS

775



### Mexican Mathematicians in the World Trends and Recent Contributions

IV Meeting
Reunión de Matemáticos Mexicanos en el Mundo
June 10–15, 2018
Casa Matemática Oaxaca
Oaxaca, Mexico

Fernando Galaz-García Cecilia González-Tokman Juan Carlos Pardo Millán Editors



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2020 Mathematics Subject Classification. Primary 53Cxx, 83Cxx, 46Lxx, 37Axx, 55Pxx, 35Cxx, 47Axx, 17Bxx, 11Fxx, 22Exx.

For additional information and updates on this book, visit www.ams.org/bookpages/conm-775

### Library of Congress Cataloging-in-Publication Data

Names: Galaz-García, Fernando, editor. | Reunión de Matemáticos Mexicanos en el Mundo (4th : 2018 : Oaxaca, Mexico)

Title: Mexican mathematicians in the world : trends and recent contributions / Fernando Galaz-García, Cecilia González-Tokman, Juan Carlos Pardo Millán, editors.

Description: Providence : American Mathematical Society, [2021] | Series: Contemporary mathematics, 0271-4132; volume 775 | Aportaciones matematicas / Sociedad Matemática Mexicana | This volume contains the proceedings of the IV Meeting of Mexican Mathematicians Abroad (IV Reunión de Matemáticos Mexicanos en el Mundo), held at Casa Matemática Oaxaca (CMO) in Oaxaca, Mexico, on June 10-15, 2018-Preface. | Includes bibliographical references. Identifiers: LCCN 2021019776 | ISBN 9781470465360 (paperback) | 9781470467289 (ebook)

Subjects: LCSH: Mathematics—Mexico—Congresses. | Mathematicians—Mexico—Congresses. | Women mathematicians—Mexico—Congresses. | AMS: Differential geometry — Global differential geometry. | Relativity and gravitational theory — General relativity. | Functional analysis — Selfadjoint operator algebras. | Dynamical systems and ergodic theory. | Algebraic topology — Homotopy theory. | Partial differential equations. | Operator theory — General theory of linear operators. | Nonassociative rings and algebras — Lie algebras and Lie superalgebras. | Number theory — Discontinuous groups and automorphic forms. | Topological groups, Lie groups.

Classification: LCC QA27.M49 M49 2021 | DDC 510.972–dc23 LC record available at https://lccn.loc.gov/2021019776

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### **Preface**

This volume contains the proceedings of the *IV Meeting of Mexican Mathematicians Abroad (IV Reunión de Matemáticos Mexicanos en el Mundo)*, held at Casa Matemática Oaxaca (CMO) in Oaxaca, Mexico, on June 10–15, 2018. This was the fourth in a series of ongoing biannual meetings connecting Mexican mathematicians residing abroad with their colleagues in Mexico. These events aim, on the one hand, at showcasing the research of Mexican mathematicians based abroad and, on the other hand, at strengthening academic connections among participants, Mexican institutions, and the broader mathematical community.

These conferences have been well received by the Mexican mathematical community, having had a visible positive impact on many levels. This can be readily seen when considering the number of new collaborations, international grant proposals, organization and participation in specialized events and, perhaps most importantly, the (re)incorporation of various speakers to Mexican academic institutions.

On this occasion, the meeting consisted of five days of activities, including 18 scientific talks, three poster sessions, three panels and discussion fora, and a public outreach talk, all supplemented with plenty of interaction time during meals and coffee breaks. This arrangement allowed for intense interactions and networking among the 53 workshop participants, who came from more than 10 countries and 10 Mexican states.

As in previous meetings, there were also opportunities for dialogue and analysis of issues relevant to the wider mathematical community and to colleagues working abroad. There was a round-table discussion on mobility, exchange, and opportunities for returning to Mexico (Movilidad, Intercambio, Reincorporación), featuring established members of the Mexican mathematical and scientific community: Alejandro Adem (University of British Columbia University), Daniel Juan (Centro de Ciencias Matemáticas, UNAM), Víctor Rivero (Centro de Investigación en Matemáticas), Gelasio Salazar (Universidad Autónoma de SLP and former President of the Mexican Mathematical Society), and Julia Tagüeña (CONACYT). In addition to this, there was an open forum led by Humberto Gutiérrez (Universidad de Guadalajara) and Silvia Reyes (Universidad Tecnológica de la Mixteca), heads of their departments of mathematics, and early-career researchers who recently joined Mexican institutions: Ana Rechtman (Instituto de Matemáticas, UNAM), Felipe García Ramos (CONACYT - Universidad Autónoma de San Luis Potosí), Alfredo Nájera (CONACYT - UNAM, Oaxaca), and Gerardo Hernández (UNAM, Juriquilla). Opportunities for graduate studies were discussed in a third forum.

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The scientific talks were recorded using BIRS video facilities and are publicly available at the workshop website

https://www.birs.ca/events/2018/5-day-workshops/18w5142.

The organizing committee was composed of a mix of mathematicians based in Mexico and abroad:

- Luz Angélica Caudillo (University of British Columbia Canada),
- Felipe García (Universidad Autónoma de San Luis Potosí, CONACYT Mexico),
- Cecilia González-Tokman (The University of Queensland, Australia),
- Xavier Gómez-Mont (CIMAT, Mexico),
- Rita Jiménez Rolland (IMATE Oaxaca, UNAM, Mexico),
- César A. Lozano (UNAM, Unidad Oaxaca, CONACYT, Mexico),
- César Maldonado (Instituto Potosino de Investigación Científica y Tecnológica, Mexico),
- Juan Pablo Maldonado (Czech Technical University, Czech Republic),
- Ana Rechtman Bulajich (Université de Strasbourg, France, and IMATE, UNAM, Mexico),
- José Antonio Seade Kuri (IMATE, UNAM, Mexico).

All the affiliations in the preceding list, as well as the affiliations in the lists of speakers and participants, are those at the time the meeting took place.

The conference was made possible thanks to the financial support of Casa Matemática Oaxaca, CONACYT, FORDECyT, Sociedad Matemática Mexicana, Instituto de Física de la UASLP, Instituto de Matemáticas de la UNAM, and the logistic support of Claudia Arias (CMO), Karla Soto (UNAM), and América Carrasco (SMM). We thank the conference speakers and the participants for their commitment to making the meeting a success, the authors and referees who contributed their time and work to these proceedings, and the editorial committees and staff of Aportaciones Matemáticas and Contemporary Mathematics for their support in preparing this volume.

Fernando Galaz-García Durham University

Cecilia González-Tokman The University of Queensland

> Juan Carlos Pardo Millán CIMAT

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Organizers at the Fourth Meeting of Mexican Mathematicians Abroad, CMO, June 10–15, 2018. (Photo by CMO)



Poster session at the Fourth Meeting of Mexican Mathematicians Abroad, CMO, June 10–15, 2018. (Photo by CMO)

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Participants at the Fourth Meeting of Mexican Mathematicians Abroad, CMO, June 10–15, 2018. (Photo by CMO)

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 $\bullet$  On the non-linear prescribed k-curvature problem on hypersurfaces of hyperbolic and anti-de sitter space

Daniel Ballesteros Chávez, Durham University (UK)

- An example of the Deligne–Mumford compactification Araceli Bonifant, University of Rhode Island (USA)
- On the Mumford-Tate conjecture for Abelian varieties
   Victoria Cantoral Farfán, International Centre for Theoretical Physics
   (Italy)
- A non-commutative topological dimension Jorge Castillejos, Katholieke Universiteit Leuven (Belgium)
- Isoperimetric and Sobolev inequalities on magnetic graphs Javier Chávez Domínguez, University of Oklahoma (USA)
- Positive Ricci Curvature and Actions of High Dimensional Tori Diego Corro Tapia, Karlsruher Institut für Technology (Germany)
- Metastable convergence of ergodic averages: the continuous logic view-point

Eduardo Dueñez, Spelman College (USA)

- Einstein metrics on 4-manifolds
   Ixchel Dzohara Gutiérrez Rodríguez, Universidad de Santiago de Compostela (Spain)
- $\bullet$  Identifying unique observations in storm super-resolved microscopic images via a spatio-temporal model

Alejandra Donaji Herrera Reyes, University of British Columbia (Canada)

- Dressing-up surfaces Alfredo Hubard, Université Marne-La Vallée (France)
- Singularly Perturbed Ordinary Differential Equations Hildeberto Jardón, Technical University Munich (Germany)

• Some connections between functional and volumetric inequalities in convex geometry

Carlos Hugo Jiménez Gómez, PUC-Rio (Brasil)

- Modelling the effect of temperature on sleep quality Alicia Prieto Langarica, Youngstown University (USA)
- Determinism and Chaos (Public Outreach Talk)
   Ana Rechtman Bulajich, Université de Strasbourg (France) and UNAM (Mexico)
- The hybridizable discontinuous Galerkin method: An application to magnetic equilibrium in fusion reactors
   Tonatiuh Sánchez-Vizuet, Courant Institute of Mathematical Sciences (USA)
- Synthetic curvature and isometries

  Jaime Santos Rodríguez, Universidad Autónoma de Madrid (Spain)
- The minimum quadratic non-residue and related problems Enrique Treviño, Lake Forest College (USA)
- The set-intersection problem and its applications Paola Vera Licona, University of Connecticut Health Center (USA)
- Microlocal and semiclassical analysis
  Alejandro Uribe, University of Michigan, Ann Arbor (USA)

### List of Participants

Alejandro Adem

University of British Columbia, Canada

Alma Rosario Arévalo Loyola

UNAM, Mexico

Daniel Ballesteros Chávez Durham University, UK

Araceli Bonifant

University of Rhode Island, USA

Victoria Cantoral Farfán

ICTP, Italy

Herón Cárdenas Cruz

Universidad Autónoma de Chiapas,

Mexico

Jorge Castillejos

Katholieke Universiteit Leuven,

Belgium

Luz Angélica Caudillo Mata

University of British Columbia, Canada

Jonathan Chávez Casillas

University of Rhode Island, USA

Javier Chávez Domínguez

University of Oklahoma, USA

Diego Corro Tapia

Karlsruher Insitut für Technologie,

Germany

Eduardo Dueñez

Spelman College, USA

Manuel Alejandro García Acosta

UNAM, Mexico

Felipe García-Ramos

Universidad Autónoma de San Luis

Potosí, Mexico

Tania Raquel Garibay Valladolid Universidad Michoacana de San Nicolás

de Hidalgo, Mexico

Cecilia González-Tokman

The University of Queensland,

Australia

Humberto Gutiérrez Pulido

Universidad de Guadalajara, Mexico

Ixchel Dzohara Gutiérrez Rodríguez

Universidade de Santiago de

Compostela, Spain

Gerardo Hernández Dueñas UNAM, Juriquilla, Mexico

Alejandra Donaji Herrera Reyes

University of British Columbia, Canada

Alfredo Hubard

Université Marne la Vallée, Paris Est,

France

Delio Jaramillo Vélez

CIMAT, Mexico

Hildeberto Jardón Kojakhmetov Technische Universität München,

Germany

Carlos Hugo Jiménez Gómez

PUC-Rio, Brazil

Rita Jiménez Rolland

UNAM, Mexico

Daniel Juan Pineda

Centro de Ciencias Matemáticas,

UNAM, Morelia, Mexico

Porfirio Leandro León Álvarez

UNAM, Mexico

Luis Lomelí Pontificia Universidad Católica de Valparaíso, Chile

César Lozano Huerta CONACYT-UNAM, Oaxaca, Mexico

César Maldonado Instituto Potosino de Investigación Científica y Tecnológica, Mexico

Miguel Maldonado Universidad Autónoma de Zacatecas, Mexico

Gari Yamel Peralta Alvarez Universidad de Colima, Mexico

Miguel Angel Prado Godoy Universidad de Guanajuato, Mexico

Alicia Prieto Langarica Youngstown State University, USA

Andrea Quintanilla Carranza Facultad de Ciencias, UNAM, Mexico

Ana Rechtman Bulajich Université de Strasbourg, France and UNAM, Mexico

Silvia Reyes Universidad Tecnológica de la Mixteca, Mexico

Mónica Andrea Reyes Quiroz Universidad Autónoma del Estado de México, Mexico

Víctor Manuel Rivero Mercado CIMAT, Mexico

Diego Rodríguez Guzmán Universidad Autónoma de Aguascalientes, Mexico

Edgardo Roldán Pensado Centro de Ciencias Matemáticas, UNAM, Morelia, Mexico

Gelasio Salazar Universidad Autónoma de San Luis Potosí, Mexico

Fernando Saldaña García CIMAT, Mexico

Tonatiuh Sánchez-Vizuet New York University, USA

Jaime Santos Rodríguez Universidad Autónoma de Madrid, Spain

Arelis Serrato Martínez Facultad de Ciencias, UNAM, Mexico

Alina Sotolongo Aguiar CIMAT, Mexico

Julia Tagüeña CONACYT, Mexico

Enrique Treviño López Lake Forest College, USA

Alejandro Uribe University of Michigan, Ann Arbor, USA

Eduardo Iván Velázquez Richards UNAM, Mexico

Paola Vera Licona University of Connecticut Health Center, USA

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- 752 Samuel Coskey and Grigor Sargsyan, Editors, Trends in Set Theory, 2020
- 751 Ashish K. Srivastava, André Leroy, Ivo Herzog, and Pedro A. Guil Asensio, Editors, Categorical, Homological and Combinatorial Methods in Algebra, 2020

Articles in this volume are based on presentations given at the IV Meeting of Mexican Mathematicians Abroad (IV Reunión de Matemáticos Mexicanos en el Mundo), held from June 10–15, 2018, at Casa Matemática Oaxaca (CMO), Mexico. This meeting was the fourth in a series of ongoing biannual meetings bringing together Mexican mathematicians working abroad with their peers in Mexico.

This book features surveys and research articles from five broad research areas: algebra, analysis, combinatorics, geometry, and topology. Their topics range from general relativity and mathematical physics to interactions between logic and ergodic theory. Several articles provide a panoramic view of the fields and problems on which the authors are currently working on, showcasing diverse research lines complementary to those currently pursued in Mexico. The research-oriented manuscripts provide either alternative approaches to well-known problems or new advances in active research fields.



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