MATHEMATICAL PROBLEMS.


This pamphlet of fifty-six pages contains solutions of more than forty problems in geometrical probability and mean values and of some other interesting mathematical problems. The solver was also the proposer of most of the problems. His solutions show skill and perseverance in evaluating many complicated definite multiple integrals.

Several problems relate to mean values of magnitudes determined by choosing random points with certain restrictions in a circle. For example, No. 11,153 is to find the average area of the dodecagon formed by joining twelve points taken at random in a circle, three in each quadrant. The expression found for this area is the quotient of two multiple integrals of twelve variables each. This is finally reduced to

\[
\frac{2^{11} \pi^2}{15 \pi^2} \left( \frac{\pi^2}{16} - \frac{704}{1575} \right) \left( 2\pi - \frac{409}{105} \right) + \frac{2^{12} \pi^3}{3 \pi^2} \left( \frac{\pi^2}{32} - \frac{86}{315} \right) \left( \frac{7\pi}{2} - \frac{853}{105} \right)
\]

Problem 11,037 is as follows:—"Two points are taken at random in the surface of a given circle. An ellipse is described on the distance between the two points as major axis. If a point be taken at random in the left-hand half of this major axis, and with this point as a centre a circle is described at random, but so as to lie wholly within the ellipse, find the average area of the ellipse described on that portion of the major axis between the right-hand extremity and the circumference of the random circle." The result obtained is

\[
\frac{\pi r^2}{1280} \left( \frac{2205\pi + 2012}{15\pi + 17} \right)
\]

This solution involves the assumption that the major axis \(a\) of an ellipse being given all possible ellipses should be included by taking the unknown minor axis as an independent variable with the limits 0 and \(a\). All possible ellipses might with equal propriety be included in other ways; as, by taking the eccentricity as the independent variable with the limits 0 and 1. The result would be altered by such a change.

Problem 11,130 implies an assumption of the same nature.
NOTES.

"A chord is drawn at random across a circle, and two points are taken at random within the circle; find the chance that both points lie on the same side of the random chord." The result $1 - \frac{128}{45\pi^2}$ is obtained by treating the distance of the chord from the centre as the independent variable. Why would it not be equally proper to take the arc subtended by the chord as the independent variable?

These problems, as stated, are indeterminate. The modes of including all possible ellipses and of choosing random chords must be fixed before the problems become definite.

It seems strange that an incorrect construction should be given for so elementary and easy a geometrical problem as No. 10,512. "Given four lines (in magnitude), construct two similar triangles each of which shall have two of the given lines as sides."

EDWARD L. STABLER.

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NOTES.

The annual meeting of the New York Mathematical Society was held Wednesday afternoon, December 30, at four o'clock, Professor Van Amringe presiding. The following persons having been duly nominated, and being recommended by the council, were elected to membership: Mr. Edwin Mortimer Blake, Columbia College; Professor Mary E. Byrd, Smith College; Professor Susan J. Cunningham, Swarthmore College; Mr. A. E. Kennely, Edison Laboratory; Mr. Alexander Kinsey, Lafayette, Ind.; Professor Anthony T. McKissick, Alabama Polytechnic Institute; Professor George D. Olds, Amherst College; Professor M. L. Pence, State College of Kentucky; Miss Amy Rayson, New York, N. Y.; Professor Benjamin Sloan, South Carolina College. The secretary reported that the membership of the Society was 210, of whom 37 lived in New York city and the immediate vicinity and were able to attend the meetings regularly. The treasurer's report having been read, an auditing committee was appointed to examine his accounts.

The nominating committee reported the following ticket for the officers and council of the Society for the ensuing year:—President, Dr. Emory McClintock; Vice-President, Professor Henry B. Fine; Treasurer, Mr. Harold Jacoby; Secretary, Dr. Thomas S. Fiske; other Members of Council, Professor J. K. Rees, Professor W. Woolsey Johnson, Professor