

- J. P. Kahane, *Une inégalité du type de Slepian et Gordon sur les processus Gaussiens*, Israel J. Math. **55** (1986), 109–110.
- B. Knaster, *Problème 4*, Colloq. Math. **1** (1947), 30–31.
- K. Mahler, *Ein Übertragungsprinzip für konvexe Körper*, Časopis Pěst. Mat. **68** (1939), 93–102.
- B. Maurey and G. Pisier, *Séries de variables aléatoires vectorielles indépendantes et propriétés géométriques des espaces de Banach*, Studia Math. **58** (1976), 45–90.
- M. Meyer and A. Pajor, *On Santaló's inequality*, GAFA Seminar, 1987–88, Lecture Notes in Math., vol. 1376, Springer-Verlag, Berlin and New York, 1989, pp. 261–263.
- V. D. Milman, *New proof of the theorem of Dvoretzky on sections of convex bodies*, Funkcional. Anal. i Priložen **5** (1971), 28–37. (Russian)
- , *Almost Euclidean quotient spaces of subspaces of a finite-dimensional normed space*, Proc. Amer. Math. Soc. **94** (1985), 445–449.
- , *Inégalité de Brunn-Minkowski inverse et applications à la théorie locale des espaces normés*, C. R. Acad. Sci. Paris **302** (1986), 25–28.
- , *On a few observations on the connections between local theory and some other fields*, GAFA Seminar, 1986–87, Lecture Notes in Math., vol. 1317, Springer-Verlag, Berlin and New York, 1988, pp. 283–289.
- G. Pisier, *Holomorphic semi-groups and the geometry of Banach spaces*, Ann. of Math. (2) **115** (1982), 375–392.
- , *Weak Hilbert spaces*, Proc. London Math. Soc. **56** (1988), 547–579.
- J. Saint-Raymond, *Sur le volume des corps convexes symétriques*, Séminaire Initiation à l'Analyse, 1980–81, Université P. et M. Curie, Paris, 1981.
- L. Santaló, *Un invariante afin para los cuerpos convexos del espacio de n dimensiones*, Portugal. Math. **8** (1949), 155–161.

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BULLETIN (New Series) OF THE
AMERICAN MATHEMATICAL SOCIETY
Volume 25, Number 1, July 1991
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0273-0979/91 \$1.00 + \$.25 per page

Exponential Diophantine equations, by T. N. Shorey and R. Tijdeman. Cambridge Tracts in Mathematics, vol. 87, Cambridge University Press, Cambridge, 1986, x + 240 pp. ISBN 0-521-26826-5

Algorithms for Diophantine equations, by B. M. M. de Weger. CWI Tract 65, Center for Mathematics and Computer Science, POB 4079, 1009 AB Amsterdam, The Netherlands, 1989, viii + 212 pp. ISBN 90-6196-375-3

Diophantine equations (named after Diophantus of Alexandria) were studied much earlier than his time, especially in China. I

was astonished to learn that the Pell equation $x^2 - Dy^2 = 1$ had been solved as early as 3000 years ago in India. The fundamental solution of $x^2 - 8y^2 - 1$ is $9 - 8 \cdot 1 = 1$. For $D = 13$, the fundamental solution is $421201 - 13 \cdot 32400 = 1$. Since this solution appears in an ancient writing, an algorithm was known in prehistoric times.

In modern times, the idea of finding solutions in positive integers has been extended. For all sorts of polynomial and exponential equations, one looks for solutions in (some fixed) number field. It is believed that the only solution of $3^x - 2^y = 1$ is given by $9 - 8 = 1$, but I know no proof. If $a, b, c > 1$, the equation $a^x - b^y = c^z$ ($x, y, z > 2$) probably has only finitely many solutions. The famous Fermat equation is a special case. It is conjectured to have no solutions.

The Thue equation is $f(x, y) = k$, $k > 0$. Here $f(x, y)$ is a homogeneous polynomial in x, y with (say) integer coefficients. Shorey and Tijdeman proved that each such equation has only finitely many solutions. De Weger gives an algorithm for finding all solutions. For reasonably small values of k the algorithm is practicable with current technology.

Another problem is: solve $x + y = z^2$, where the prime divisors of xy are restricted to be among 2, 3, 5, 7. De Weger tabulates all solutions. The largest is $2^3 3^7 5^4 7 + 1 = 13^2 673^2$. Other large ones are $2^{12} + 3^3 \cdot 5 \cdot 7 = 71^2$, $2^5 3^2 5^2 7 + 1 = 449^2$. The smallest are $3 + 1 = 4$, $2 + 2 = 4$.

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BULLETIN (New Series) OF THE
AMERICAN MATHEMATICAL SOCIETY
Volume 25, Number 1, July 1991
©1991 American Mathematical Society
0273-0979/91 \$1.00 + \$.25 per page

Volterra integral and functional equations, by G. Gripenberg, S.-O. Londen, and O. Staffans. Cambridge University Press, Cambridge, 1990, 701 pp., \$99.50. ISBN 0-521-37289-5

The spirit of this book is captured in the following quotation from the introduction "The subject of Volterra equations in finite