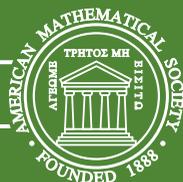


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# BULLETIN

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OF THE

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AMERICAN MATHEMATICAL SOCIETY

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BULLETIN OF THE AMERICAN MATHEMATICAL SOCIETY  
CONTENTS

Vol. 39, No. 2

April 2002

BULLETIN ARTICLES

<b>John C. Baez</b> , The octonions .....	145
<b>Ivar Ekeland and Nassif Ghoussoub</b> , Selected new aspects of the calculus of variations in the large .....	207

BOOK REVIEWS

<b>Roger W. Carter</b> (Reviewer), Characters of finite Coxeter groups and Iwahori-Hecke algebras by Meinolf Geck and Götz Pfeiffer .....	267
<b>Bruce Kleiner</b> (Reviewer), Lectures on spaces of nonpositive curvature by W. Ballmann; Metric spaces of non-positive curvature by Martin R. Bridson and André Haefliger; Geometry of nonpositively curved manifolds by Patrick B. Eberlein .....	273
<b>Toshikazu Sunada</b> (Reviewer), Random walks on infinite graphs and groups by Wolfgang Woess .....	281
<b>Bent Orsted</b> (Reviewer), Holomorphy and convexity in Lie theory by Karl- Hermann Neeb .....	287
<b>W. Duke</b> (Reviewer), Character sums with exponential functions and their applications by S. Konyagin and I. Shparlinski .....	293
<b>Alexander Lubotzky</b> , Erratum to “New horizons in pro- $p$ groups” .....	299



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