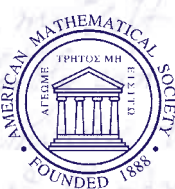


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BULLETIN OF THE AMERICAN MATHEMATICAL SOCIETY
CONTENTS

Vol. 44, No. 2

April 2007

ARTICLES

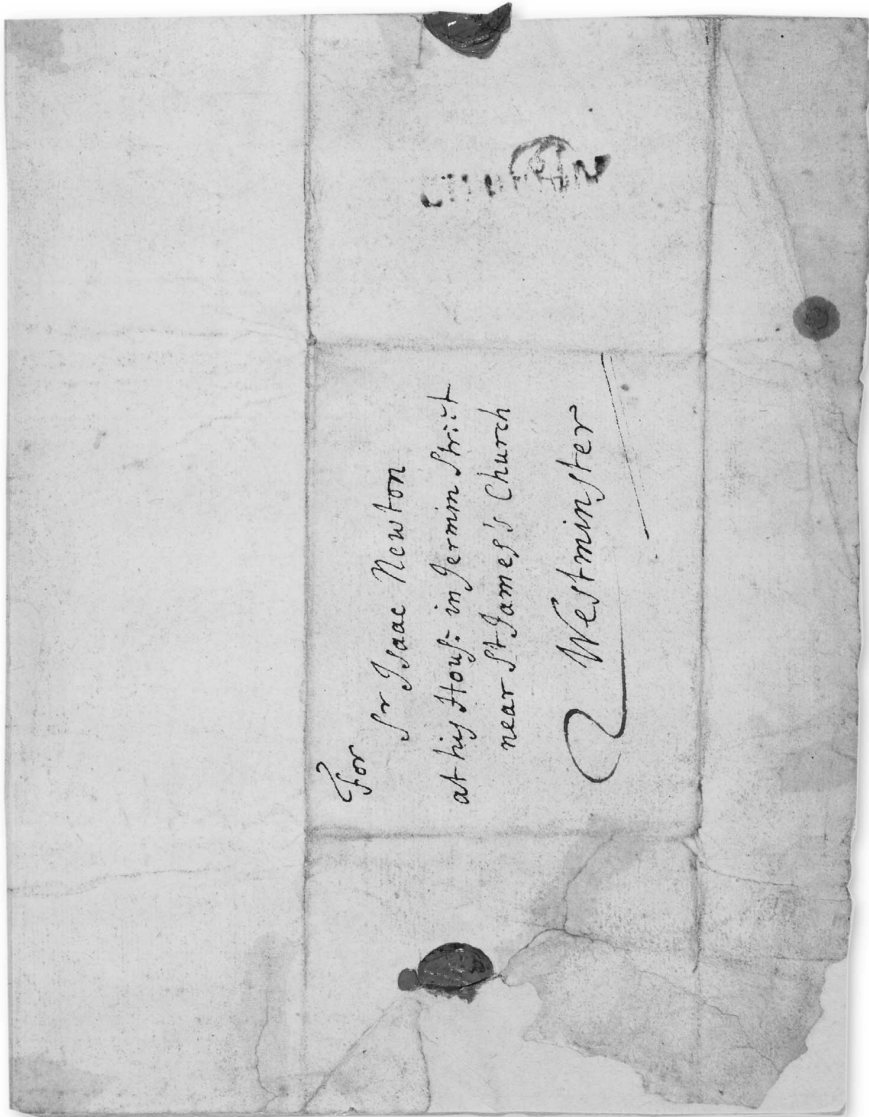
Juha Heinonen , Nonsmooth calculus	163
Baur Bektemirov, Barry Mazur, William Stein, and Mark Watkins , Average ranks of elliptic curves: Tension between data and conjecture	233

MATHEMATICAL PERSPECTIVES

Susan Friedlander , About the cover: Isaac Newton and Roger Cotes	255
Selected Mathematical Reviews	259

BOOK REVIEWS

Christopher J. Bishop (Reviewer), Harmonic measure , by John B. Garnett and Donald E. Marshall	267
Nicholas J. Higham (Reviewer), Spectra and pseudospectra: The behavior of nonnormal matrices and operators , by Lloyd N. Trefethen and Mark Embree	277
Karlheinz Gröchenig (Reviewer), Time-frequency and time-scale methods , by Jeffrey A. Hogan and Joseph D. Lakey	285
R. P. Langlands (Reviewer), p-Adic automorphic forms on Shimura varieties , by Haruzo Hida	291
Yakov Eliashberg (Reviewer), J-holomorphic curves and symplectic topology , by Dusa McDuff and Dietmar Salamon	309
Kathleen T. Alligood (Reviewer), The theory of chaotic attractors , edited by Brian R. Hunt, Judy A. Kennedy, Tien-Yien Li, and Helena E. Nusse	317
Rafe Mazzeo (Reviewer), Non-linear elliptic equations in conformal geometry , by S.-Y. Alice Chang	323



For Sir Isaac Newton
at his Houſe in Jermin Street
near St James's Church
Westminster

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BULLETIN OF THE AMERICAN MATHEMATICAL SOCIETY
CONTENTS

Vol. 44, No. 2

April 2007

ARTICLES

- Juha Heinonen**, Nonsmooth calculus 163
Baur Bektemirov, Barry Mazur, William Stein, and Mark Watkins,
 Average ranks of elliptic curves: Tension between data and conjecture 233

MATHEMATICAL PERSPECTIVES

- Susan Friedlander**, About the cover: Isaac Newton and Roger Cotes 255
 Selected Mathematical Reviews 259

BOOK REVIEWS

- Christopher J. Bishop** (Reviewer), Harmonic measure, by John B. Garnett
 and Donald E. Marshall 267
Nicholas J. Higham (Reviewer), Spectra and pseudospectra: The behavior
 of nonnormal matrices and operators, by Lloyd N. Trefethen and Mark
 Embree 277
Karlheinz Gröchenig (Reviewer), Time-frequency and time-scale methods,
 by Jeffrey A. Hogan and Joseph D. Lakey 285
R. P. Langlands (Reviewer), p -Adic automorphic forms on Shimura
 varieties, by Haruzo Hida 291
Yakov Eliashberg (Reviewer), J -holomorphic curves and symplectic
 topology, by Dusa McDuff and Dietmar Salamon 309
Kathleen T. Alligood (Reviewer), The theory of chaotic attractors, edited
 by Brian R. Hunt, Judy A. Kennedy, Tien-Yien Li, and Helena E. Nusse 317
Rafe Mazzeo (Reviewer), Non-linear elliptic equations in conformal
 geometry, by S.-Y. Alice Chang 323



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