INTRODUCTORY COMMENTS

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As the readers will observe, this issue of the *Bulletin of the American Mathematical Society* is somewhat unusual. All the articles concern topology. Last year John Milnor sent me the draft of an article based on his Abel lecture at the 2014 International Congress of Mathematicians in Seoul and inquired if it might fit in the *Bulletin* even though it is written in a very non-standard style. The Editors decided that this “lightning tour” of topology, concentrating on low dimensional manifolds, by a mathematician who made so many seminal contributions to topology would indeed appeal to the readers of the *Bulletin*. We then began to put together a whole issue related to certain aspects of John Milnor’s work.

The items in the Articles section of this issue of the *Bulletin* are the following:

4. Selected letters in the correspondence between Michel Kervaire and John Milnor over the period 1958–1961. Comments on this correspondence, which is now in the Kervaire Nachlass, are given by Andrew Ranicki and Claude Weber.

Thus the narrative of this issue begins with the most recent International Congress of Mathematicians in Seoul and moves backwards in time to the 1962 ICM in Stockholm where Milnor was awarded a Fields Medal. The citation given by Hassler Whitney on this occasion begins with the observation that the research in the 1950s by Milnor and others opened a vast field of work which now acquired a name: differential topology. Whitney concludes with the words “Differential topology is a strong young field with a bright present and a great outlook, and that its vitality is largely due to the fine achievements of Milnor.”

The list of Milnor’s articles in his collected works on what are called exotic spheres begins with a 1956 paper that Whitney remarks astounded the mathematical world, namely his proof that the 7-sphere was capable of several differential structures. The list concludes with the famous 1963 paper by Kervaire and Milnor, “Groups of homotopy spheres: I”. We reprint Milnor’s own discussion as to how these exotic sphere papers came to be written. We then present some previously unpublished material related to this paper, namely items from the correspondence...
between Kervaire and Milnor over the period of their collaboration from 1958 to 1961 that preceded the writing of their 1963 article. We conclude this section by reproducing in full the Kervaire–Milnor article that originally appeared in the *Annals of Mathematics*, vol. 77, no. 3, May 1963.

The Mathematical Perspectives section of this issue contains selected Mathematical Reviews. Our choice begins with the very lucid review by Frank Adams of the 1963 Kervaire–Milnor article and continues with reviews of papers that show the development of the subject in later years.

In this issue the *Bulletin* readers have a rare chance to see behind the scenes of a collaboration that produced one of the most influential articles of 20th century topology. Nowadays letters between collaborators have been replaced by such useful tools as e-mail, skype, dropbox, polymath, etc. We hope 21st century mathematicians will find the “old fashioned” Kervaire–Milnor correspondence illuminating.

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Photo of John Milnor from 1965 that appears with the Kervaire–Milnor *Annals* article.

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Photo of Michel Kervaire from 1956 that appears with the Kervaire–Milnor *Annals* article.


**John W. Milnor**


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