

# BULLETIN

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AMERICAN MATHEMATICAL SOCIETY

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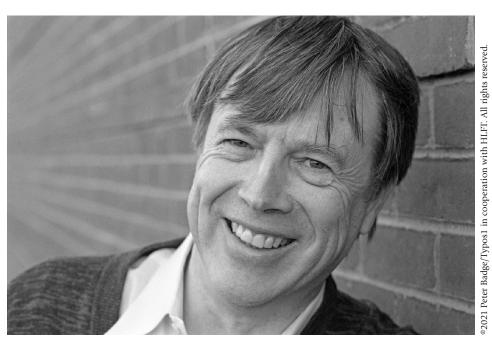
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Jean Bourgain (1954–2018)

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