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Yuri Ivanovich Manin (1937–2023)

Honors and Awards include Brouwer Medal (1987) Nemmers Prize in Mathematics (1994) Rolf Schock Prize of the Royal Swedish Academy of Sciences (1999) Cantor Medal of the Deutsche Mathematiker-Vereinigung (2002) King Faisal International Prize (2002) International János Bolyai Prize of Mathematics (2010)

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