

## UNPUBLISHED MATHEMATICAL TABLES

122[B].—H. E. SALZER, *Table of  $n!/x^{n+1}$* . Manuscript in possession of the author, NBSCL.

This table gives, to within a unit in the 9th place, the values of the function  $n!/x^{n+1}$  for  $n = 0(1)10$  and  $x = .1(.1)10$ . The table was computed with the aid of PETERS & STEIN's values of the powers of the reciprocals on p. 36–57 of the *Anhang* to J. PETERS, *Zehnstellige Logarithmentafel*, v. 1.

123[F].—A. GLODEN, *Factorization of  $2n^2 + 1$  for  $n = 1(1)1000$* . Typewritten manuscript of 11 leaves deposited in UMT FILE and Scientific Computing Service, London, and in possession of the author, 11 rue Jean Jaurès, Luxembourg.

A table extending to  $n = 3000$  is contemplated by the author.

124[F].—A. GLODEN, *Tables of Quadratic Partitions  $p = a^2 + 3b^2$  for  $100000 < p < 200000$* . Typewritten manuscript of 18 leaves, deposited as in UMT 123.

The argument  $p$  is a prime of the form  $6m + 1$ . The table gives  $a$  and  $b$  for each  $p$  with some 35 omissions which are promised in an addendum [for previous tables up to  $p = 125000$  see RMT 883].

125[F].—R. M. ROBINSON, *Tables of Integral Solutions of  $|y^2 - x^3| < x$  for  $x < 10^6/9$* . Tabulated from punched cards and deposited in the UMT FILE. Cards in possession of the author, University of California, Berkeley.

There are 5 tables. The first gives all solutions arranged according to  $x$ , of which there are 1242. Table II lists the 332 cases in which  $y^2 = x^3$ . Table III is arranged in order of  $|y^2 - x^3|$ . Table IV is for  $y^2 > x^3$  and Table V is for  $y^2 < x^3$ . Tables IV and V omit the trivial solutions  $x = 4k^2 \pm 1$ ,  $y = 8k^3 \pm 3k$ , which are starred in Tables I and III.

126[L].—G. FLAKE & Y. L. LUKE, *Tables of the Function  $(1 - uZ)^{-1/u}$* . Lithographed manuscript, 4 leaves, deposited in UMT FILE and available from Midwest Research Institute, 4049 Pennsylvania Ave., Kansas City, Mo.

The table gives 8D values of this function for

$$z = .7(.01)1.25, \quad u = .09(.01).12.$$

127[L].—C. P. GREEN, J. H. LILLIE & D. W. RAYNOLDS, *Extensive Tables of the Exponential Integral*. A thesis, Chemical Engineering Dept., Univ. of Tennessee. Knoxville, 1951, xxv + 111 leaves.

The main table is of  $-Ei(-x)$  for  $x = 15(.0001)16$ . There are also tables of  $Ei(x)$  and  $-Ei(-x)$  for  $x = 15(1)50$  and interpolation coefficients as introduced by COULSON & DUNCANSON [*Phil. Mag.*, s. 7, v. 33, 1942, p. 745–760].

128[L].—G. JONES & D. UFFORD, *Table of the Functions*  $C(P) = K_1(P)/[K_1(P) + K_0(P)]$  and of  $PC'(P)$ . Lithographed manuscript, 4 leaves, available as in UMT 126.

$K_1$  and  $K_0$  are the usual Bessel functions. The tables give  $C(P)$  and  $-PC'(P)$  to 7D for  $P = 0(.002).1(.01).3(.02)1(.1)2(.5)10(10)100$ , and also for  $P = .35(.05).95$ .

129[L].—Y. L. LUKE & D. UFFORD, *Tables of the Function*  $\bar{K}_0(x) = \int_0^x K_0(t) dt$ . Lithographed manuscript, 3 leaves, deposited as in UMT 126.

The table gives 8D values of  $\bar{K}_0(x)$  and of the auxiliary functions  $A_1(x)$  and  $A_2(x)$  defined by

$$K_0(x) = (\ln 2 - \gamma - \ln x)A_1(x) + A_2(x)$$

for  $x = 0(.01).5(.05)1$ .

130[L].—UNIVERSITY OF TORONTO COMPUTATION CENTRE, *Tables of Spherical Bessel Functions for Semi-imaginary Argument*. Photo copy, 2 leaves deposited in UMT FILE.

The tables give 8S values of the real and imaginary parts, absolute values and arguments of

$$\begin{aligned} (2x/\pi)^{-\frac{1}{2}}e^{-\pi i/4} J_{n+\frac{1}{2}}(xe^{\pi i/2}) \\ (2x/\pi)^{-\frac{1}{2}}e^{-\pi i/4} Y_{n+\frac{1}{2}}(xe^{\pi i/2}) \end{aligned}$$

for  $n = 0, 1, 2, 3; x = 0(1)10$ .

### AUTOMATIC COMPUTING MACHINERY

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#### *Notes on Numerical Analysis—5*

##### *Table-Making for Large Arguments. The Exponential Integral*

The evaluation of a function defined by a definite integral, for the complete range of argument  $-\infty$  to  $+\infty$ , is usually performed in several stages. For small and moderate values of the argument  $x$  the integral is evaluated by means of an ascending series in powers of  $x$ , or perhaps by numerical quadrature. For very large values of  $x$ , numerical values are obtained by means of an asymptotic series.

The exponential integral, for example, defined by the equations

$$\begin{aligned} \text{Ei}(x) &= \int_{-\infty}^x t^{-1}e^t dt \\ -\text{Ei}(-x) &= \int_x^{\infty} t^{-1}e^{-t} dt \end{aligned} \tag{1}$$