

UNPUBLISHED MATHEMATICAL TABLES

122[B].—H. E. SALZER, *Table of $n!/x^{n+1}$* . Manuscript in possession of the author, NBSCL.

This table gives, to within a unit in the 9th place, the values of the function $n!/x^{n+1}$ for $n = 0(1)10$ and $x = .1(.1)10$. The table was computed with the aid of PETERS & STEIN's values of the powers of the reciprocals on p. 36–57 of the *Anhang* to J. PETERS, *Zehnstellige Logarithmentafel*, v. 1.

123[F].—A. GLODEN, *Factorization of $2n^2 + 1$ for $n = 1(1)1000$* . Typewritten manuscript of 11 leaves deposited in UMT FILE and Scientific Computing Service, London, and in possession of the author, 11 rue Jean Jaurès, Luxembourg.

A table extending to $n = 3000$ is contemplated by the author.

124[F].—A. GLODEN, *Tables of Quadratic Partitions $p = a^2 + 3b^2$ for $100000 < p < 200000$* . Typewritten manuscript of 18 leaves, deposited as in UMT 123.

The argument p is a prime of the form $6m + 1$. The table gives a and b for each p with some 35 omissions which are promised in an addendum [for previous tables up to $p = 125000$ see RMT 883].

125[F].—R. M. ROBINSON, *Tables of Integral Solutions of $|y^2 - x^3| < x$ for $x < 10^6/9$* . Tabulated from punched cards and deposited in the UMT FILE. Cards in possession of the author, University of California, Berkeley.

There are 5 tables. The first gives all solutions arranged according to x , of which there are 1242. Table II lists the 332 cases in which $y^2 = x^3$. Table III is arranged in order of $|y^2 - x^3|$. Table IV is for $y^2 > x^3$ and Table V is for $y^2 < x^3$. Tables IV and V omit the trivial solutions $x = 4k^2 \pm 1$, $y = 8k^3 \pm 3k$, which are starred in Tables I and III.

126[L].—G. FLAKE & Y. L. LUKE, *Tables of the Function $(1 - uZ)^{-1/u}$* . Lithographed manuscript, 4 leaves, deposited in UMT FILE and available from Midwest Research Institute, 4049 Pennsylvania Ave., Kansas City, Mo.

The table gives 8D values of this function for

$$z = .7(.01)1.25, \quad u = .09(.01).12.$$

127[L].—C. P. GREEN, J. H. LILLIE & D. W. RAYNOLDS, *Extensive Tables of the Exponential Integral*. A thesis, Chemical Engineering Dept., Univ. of Tennessee. Knoxville, 1951, xxv + 111 leaves.

The main table is of $-Ei(-x)$ for $x = 15(.0001)16$. There are also tables of $Ei(x)$ and $-Ei(-x)$ for $x = 15(1)50$ and interpolation coefficients as introduced by COULSON & DUNCANSON [*Phil. Mag.*, s. 7, v. 33, 1942, p. 745–760].

128[L].—G. JONES & D. UFFORD, *Table of the Functions* $C(P) = K_1(P)/[K_1(P) + K_0(P)]$ and of $PC'(P)$. Lithographed manuscript, 4 leaves, available as in UMT 126.

K_1 and K_0 are the usual Bessel functions. The tables give $C(P)$ and $-PC'(P)$ to 7D for $P = 0(.002).1(.01).3(.02)1(.1)2(.5)10(10)100$, and also for $P = .35(.05).95$.

129[L].—Y. L. LUKE & D. UFFORD, *Tables of the Function* $\bar{K}_0(x) = \int_0^x K_0(t) dt$. Lithographed manuscript, 3 leaves, deposited as in UMT 126.

The table gives 8D values of $\bar{K}_0(x)$ and of the auxiliary functions $A_1(x)$ and $A_2(x)$ defined by

$$K_0(x) = (\ln 2 - \gamma - \ln x)A_1(x) + A_2(x)$$

for $x = 0(.01).5(.05)1$.

130[L].—UNIVERSITY OF TORONTO COMPUTATION CENTRE, *Tables of Spherical Bessel Functions for Semi-imaginary Argument*. Photo copy, 2 leaves deposited in UMT FILE.

The tables give 8S values of the real and imaginary parts, absolute values and arguments of

$$\begin{aligned} (2x/\pi)^{-\frac{1}{2}}e^{-\pi i/4} J_{n+\frac{1}{2}}(xe^{\pi i/2}) \\ (2x/\pi)^{-\frac{1}{2}}e^{-\pi i/4} Y_{n+\frac{1}{2}}(xe^{\pi i/2}) \end{aligned}$$

for $n = 0, 1, 2, 3; x = 0(1)10$.

AUTOMATIC COMPUTING MACHINERY

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Notes on Numerical Analysis—5

Table-Making for Large Arguments. The Exponential Integral

The evaluation of a function defined by a definite integral, for the complete range of argument $-\infty$ to $+\infty$, is usually performed in several stages. For small and moderate values of the argument x the integral is evaluated by means of an ascending series in powers of x , or perhaps by numerical quadrature. For very large values of x , numerical values are obtained by means of an asymptotic series.

The exponential integral, for example, defined by the equations

$$\begin{aligned} \text{Ei}(x) &= \int_{-\infty}^x t^{-1}e^t dt \\ -\text{Ei}(-x) &= \int_x^{\infty} t^{-1}e^{-t} dt \end{aligned} \tag{1}$$