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and other
Aids to Computation

A Quarterly Journal

Edited by

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C. C. CRAIG
A. ERDÉLYI
F. J. MURRAY
J. TODD
D. H. LEHMER, *Chairman*

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CONTENTS

VI NUMBER 37 JANUARY 1952

The Difference Analyzer: A Simple Differential Equation Solver..... G. A. KORN 1

An Extension of Gauss' Transformation for Improving the Condition of Systems of Linear Equations..G. E. FORSYTHE & T. S. MOTZKIN 9

Recent Mathematical Tables..... 18

ABRAMOWITZ **947**, BIZLEY **933**, BOGERT **948**, BRL **958**, COMP. DEPT. MATH. CENTER, AMSTERDAM **949**, DEMING **941**, DIXON **942**, DWYER **960**, GRÖBNER & HOFREITER **950**, GUMBEL & GREENWOOD **943**, GUPTA **937**, IMAI & HASIMOTO **959**, KATZ **938**, LUKE & DENGLER **951**, MASSEY **944**, MASSEY **945**, NBSCL **952**, NEĬSHULER **934**, PETSCHACHER **953**, PÓLYA & SZEGÖ **954**, REITWIESNER **955**, RICCI **956**, SALZER **957**, SELMER **939**, SICHEL **946**, TODD **936**, UHLER **935**, ZAVROTSKY **940**.

Mathematical Tables—Errata..... 35

BIRGE **198**, FISHER & YATES **199**, INGHIRAMI **200**, NIELSEN & GOLDSTEIN **201**, VINOGRADOV & CHETAEV **202**.

Unpublished Mathematical Tables..... 39

BRINKLEY, EDWARDS & SMITH **141**, FERRIER **136**, FERRIER **137**, GUEST **140**, HIGA **142**, JOHNSON **138**, LUKE **143**, POLETTI **139**.

Automatic Computing Machinery..... 41

Technical Developments, Fundamental Concepts of the Digital Differential Analyzer Method of Computation....R. E. SPRAGUE
Bibliography Z–XVIII: ANON **1–2**, GILL **3**, OFFICE OF NAVAL RESEARCH **4**, RATZ & SMITH **5**, TILLMAN **6**, TUTTLE **7**, WILKES, WHEELER & GILL **8**
News

Other Aids to Computation..... 55

Bibliography Z–XVIII: ACKERMAN **9**, ANON. **23**, BADER **10**, BÜCKNER **11**, CARROLL & BENNETT **12**, CASTORE & DYE **13**, CHARP **14**, CROWELL **15**, DREYER **16**, JAREMA **17**, KRIENES **18**, LYON **19**, MERIAM **20**, MOORE **21**, RAMSAYER **22**, SAY **24**, WALKER **25**

Notes..... 58

129. Zeros of $I_{n+1}(x)J_n(x) + J_{n+1}(x)I_n(x)$.....G. BLANCH

130. A Method of Factorisation Using a High-Speed Computer.....G. G. ALWAY

131. Recent Discoveries of Large Primes.....D. H. LEHMER

Queries..... 61

Corrigenda..... 61

CONTENTS

VI NUMBER 38 APRIL 1952

The Use of Exponential Sums in Step by Step Integration..... P. BROCK & F. J. MURRAY 63

A note on the Inversion of Matrices by Random Walks..W. R. WASOW 78

Recent Mathematical Tables..... 81

ABRAMOWITZ **981**, BLOCH, HULL, BROYLES, BOURICIUS, FREEMAN & BREIT **982**, BLOMQVIST **964**, BROCKMEYER **965**, BROCKMEYER, HALSTRØM & JENSEN **966**, BUEHLER & HIRSCHFELDER **983**, COOK **967**, CROSSLEY **984**, DAVID, KENDALL & STUART **968**, DEAN **985**, DURBIN & WATSON **969**, EMERSLEBEN **986**, GAYEN **970**, GORDON **987**, GRONOW **971**, GUMPRECHT & SLIEPCEVICH **989**, KEEPING **972**, KUHN **988**, KULIK, POLETTI & PORTER **962**, OLVER **990**, PACKER **973**, PEARSON & MERRINGTON **974**, PILLAI **975**, RAFF **976**, RIDER **977**, SHRIKHANDE **978**, SHUMÎAGSKIĬ **963**, SIEGEL, BROWN, HUNTER, ALPERIN & QUILLEN **991**, SPENCER & REYNOLDS **961**, SPRINGER **979**, WHITNEY **980**.

Mathematical Tables—Errata..... 99

AKADEMIIA NAUK **203**, BAASMTC **204**, MCLACHLAN & HUMBERT **205**, MCLACHLAN, HUMBERT & POLI **206**, OBERG & JONES **207**, PEARSON **208**, USPENSKY **209**.

Unpublished and Mathematical Tables..... 102

GLODEN & BONNEAU **144**, LEHMER **145**, **146**.

Automatic Computing Machinery..... 102

Technical Developments, The Serial-Memory Digital Differential Analyzer.....J. F. DONAN

Discussions, The Adventures of a Blunder.....R. A. BROWN, S. GILL & D. J. WHEELER

Bibliography Z–XIX: ANON. **1–2**, BRINKLEY **3**, BRAUGH, SCHLINGER & SAGE **4**, DONNELL & DRAPER **5**, GOODMAN **6**, KING **7**, MARTIN & YACHTER **8**, OPLER & HEITZ **9**, ROSE, JOHNSON & WILLIAMS **10**, ROSE, LOMBARDO & WILLIAMS **11**, ROSE, WILLIAMS & KAHN **12**.

News

Other Aids to Computation..... 119

Bibliography Z–XIX: ANON. **13–16**, BOHO **17**, CHANCE, WILLIAMS, YANG, BUSSER & HIGGINS **18**, CONNOLLY, FRANKEL & SAGE **19**, CORTELYOU **20**, EVERITT **21**, GOODE **22**, HARRINGTON **23**, JAEGER **24**, JEFFERSON & ERICSSON **25**, KENNEDY **26**, LAKATOS **27**, LLEWELLYN **28**, MACADAM **29**, ROBERTSON **30**, UNGAR **31**, VAND **32**, WATERS **33**, WINKLER **34**.

Notes..... 123

132. Further Statistics on the Digits of e.....F. GRUENBERGER

133. On Finding the Electronic Cycle Capacity of the IBM Type 604 Computer.....A. O. RIDGWAY

134. Fritz Emde.....R. C. ARCHIBALD

135. Ralph Ernest Powers.....D. H. LEHMER

Queries..... 125

Corrigenda..... 126

CONTENTS

VI NUMBER 39 JULY 1952

Use of Continued Fractions in High Speed Computing . . D. TEICHROEW 127

On a Punched-Card Method of Solving Certain Integral Equations . . . . . B. A. GRIFFITH & K. W. SMILLIE 133

The Use of Exponential Sums in Step by Step Integration—II . . . . . P. BROCK & F. J. MURRAY 138

Recent Mathematical Tables 150

AULUCK **995**, BAASMTC **993**, BIRNBAUM & TINGEY **999**, BLOMQVIST **998**, CHAMBERS **1000**, DAVIS **1018**, DITKIN & KUZNETSOV **1009**, EMERSLEBEN **1010**, GOUSSINSKY **994**, HAGEN **1011**, HAMMERSLEY **1012**, HOWARTH **1013**, LINDER **1001**, MIDDLETON & JOHNSON **1014**, MORIGUTI **1002**, NATH **1003**, POWELL **1015**, RIDER **1004**, RIORDAN **996**, SALZER **997**, SPENCELEY, SPENCELEY & EPPERSON **992**, STEVENS **1005**, THOMAS **1006**, VAN DER VAART **1007**, WALSH **1008**, WEINBERG **1016**, WILKINS **1017**.

Mathematical Tables—Errata 163

ARENBERG & LEVIN **210**, BOSE **211**, KULIK, POLETTI & PORTER **212**, RHETICUS-PITISCUS **213**.

Unpublished Mathematical Tables 167

GLODEN **149**, GRUENBERGER **148**, STORCH **147**.

Automatic Computing Machinery 167

Technical Developments, An Automatic Computer in Australia . . . . . T. PEARCEY

Discussions, Minimum Access Programming . . . . . D. P. PERRY

Bibliography Z–XX: ALLEN & STARK **1**, ALT **2**, ANON. **3**, AUERBACH, ECKERT, SHAW, WEINER & WILSON **4**, COZZONE **5**, DONNELL **6**, FEDER **7**, GOODE **8**, GRAY **9**, KAZAN & KNOLL **10**, LEPHAKIS **11**, OFFICE OF NAVAL RESEARCH **12**, RUTISHAUSER, SPEISER & STIEFEL **13**.

Other Aids to Computation 190

Linear Algebraic Systems and the REAC . . . . . L. GEPHART

Notes 204

136. Solution of $y = e^y$ . . . . . R. C. ARCHIBALD

137. Punched Card Tables . . . . . G. BLANCH & E. C. YOWELL

138. A New Mersenne Prime . . . . . D. H. L.

Query 205

Queries—Replies 205

CONTENTS

VI NUMBER 40 OCTOBER 1952

The Office of Naval Research Relay Computer ..... J. JAY WOLF 207

On the Rounding Off of Difference Tables for Linear Interpolation .. .. A. M. OSTROWSKI 212

Mechanical Quadrature Near a Singularity ..... YUDELL L. LUKE 215

On the Numerical Solution of Equations Involving Differential Operators with Constant Coefficients ..... GERTRUDE BLANCH 219

Recent Mathematical Tables 224

CHANDRASEKHAR, ELBERT & FRANKLIN **1030**, CHESTER **1031**, DAVID **1023**, DAVID & KENDALL **1020**, DIEMER & DIJKGRAAF **1032**, DRAGONETTE **1019**, GOLDSTEIN **1033**, GRUNDY **1024**, GUEST **1025**, HARTLEY & PEARSON **1026**, HARVARD UNIV. COMP. LAB. **1034**, KAARSEMAKER & VAN WIJNGAARDEN **1027**, KOPAL, CARRUS & KAVANAGH **1022**, LAIBLE **1035**, LING **1036**, LOCK **1037**, MISHRA **1038**, OSIMA **1021**, PAPOULIS **1039**, PETERS **1018**, PILLAI **1028**, VAN WIJNGAARDEN **1040**, WALSH **1029**, WILSON **1041**.

Mathematical Tables—Errata 236

ADAMS & HIPPISLEY **214**, GERSHUN **215**, GOLDSTEIN **215**, JAHNKE & EMDE **216**, PIPPING **217**, SCHMIDT **215**.

Unpublished Mathematical Tables 238

WALL **150**.

Automatic Computing Machinery 238

Discussions, Asynchronous Signals in Digital Computers ..... S. LUBKIN

Bibliography Z–XXI: ANON. **1–2**, BARNES, COOKE-YARBOROUGH & THOMAS **3**, GEISLER **4**, GOETZ & BROOKE **5**, MUTTER **6**, REY **7**, WILD **8**.

News

Other Aids to Computation 248

Bibliography Z–XXI: ANON. **9**, CURRIE **10**, GRANDI & LEBELL **11**, JAMES **12**, JOHNSON **13**, LAKATOS **14**, LEE & WIESNER **15**, MACNEE **16**, SCOTT **17**, SHAH & JACOBS **18**, SOKOLOFF **19**, TAUXE & STOKER **20**.

Notes 251

139. The RAND Collection of Illustrative Approximations ..... C. HASTINGS, JR.

140. An Alternative "Predictor-Corrector" Process ..... T. H. SOUTHARD & E. C. YOWELL

141. A New Calculation of Euler's Constant .. J. W. WRENCH, JR.

142. The Determination of a Large Prime ..... A. FERRIER

Queries—Replies 257

Corrigenda 257

Indices 258

CLASSIFICATION OF TABLES

A. Arithmetical Tables. Mathematical Constants

B. Powers

C. Logarithms

D. Circular Functions

E. Hyperbolic and Exponential Functions

F. Theory of Numbers

G. Higher Algebra

H. Numerical Solution of Equations

I. Finite Differences. Interpolation

J. Summation of Series

K. Statistics

L. Higher Mathematical Functions

M. Integrals

N. Interest and Investment

O. Actuarial Science

P. Engineering

Q. Astronomy

R. Geodesy

S. Physics, Geophysics, Crystallography

T. Chemistry

U. Navigation

V. Aerodynamics, Hydrodynamics, Ballistics

Z Calculating Machines and Mechanical Computation