

where $C_1 = 1 - \gamma$, $\gamma = \lim \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{n} - \log n \right)$: Euler's constant

$$C_r = \frac{1}{r} \left(\frac{1}{2^r} + \frac{1}{3^r} + \frac{1}{4^r} + \dots \right) \quad (r = 2, 3, \dots).$$

The values of $S_r = \frac{1}{1^r} + \frac{1}{2^r} + \frac{1}{3^r} + \dots$ and γ were taken from Stieltjes' table.¹

Part of the calculation was done with the assistance of Mr. E. V. HANKAM on an IBM (602-A type) calculating punch. Uhler's radix table was used for getting the antilog of $\log \Gamma$. The values $\Gamma(\frac{1}{3})$ and $\Gamma(\frac{2}{3})$ were required for calculating the power series coefficients of Bessel functions of order $\frac{1}{3}$ and of functions related to them.

The values were checked by the identity

$$\sqrt{3}\Gamma(\frac{1}{3})\Gamma(\frac{2}{3}) = 2\pi$$

$\Gamma(\frac{1}{3}) =$	2.67893	85347	07747	63365	56929	410
$\Gamma(\frac{2}{3}) =$	1.35411	79394	26400	41694	52880	282
$\log \Gamma(\frac{1}{3}) =$.98542	06469	27767	06918	71740	370
$\log \Gamma(\frac{2}{3}) =$.30315	02751	47523	56867	58628	174

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¹ H. T. DAVIS, *Tables of Higher Mathematical Functions*. v. II, The Principia Press, 1935, p. 244.

Modification of a Method for Calculating Inverse Trigonometric Functions

The 605 programming that I gave recently¹ fails for arguments near 2^{-1} . The reason for this failure is that the double angle formulations used multiply round-off errors until they are intolerably large. These formulations were originally introduced to assure that $\cos 2\theta$ depend on both $\sin \theta$ and $\cos \theta$. Upon closer examination it was found that it is only necessary that $\cos 2\theta$ depend on $\sin \theta$, hence we may use

$$\cos 2\theta = 1 - 2 \sin^2 \theta.$$

The use of the above formula and

$$\sin 2\theta = 2 \sin \theta \cos \theta$$

avoids the errors mentioned and is just as easily programmed for the 605.

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¹ RICHARD L. LA FARA, *MTAC*, v. 8, 1954, p. 132-139.