

## ERRATUM: “ON THE COMPUTATION OF LOCAL COMPONENTS OF A NEWFORM”

DAVID LOEFFLER AND JARED WEINSTEIN

ABSTRACT. It has been brought to our attention that there is an error in Section 4 of our article, *On the computation of local components of a newform*, Math. Comp. 81, 2012. We briefly explain how this error can be corrected.

Proposition 4.1(1) of our article [2] is not correct as stated. For instance, if  $\varepsilon$  is the quadratic Dirichlet character of conductor 15, then there are two newforms in  $S_3(\Gamma_1(15), \varepsilon)$  with coefficients in  $\mathbf{Q}$ , and these are twists of each other by the quadratic character of conductor 3, whereas the quantity  $u$  in the proposition is 0 here. We are grateful to Steve Donnelly of the University of Sydney for pointing out this counterexample.

The correct statement is the following. Let  $f$  be a newform of level  $Np^r$ , with  $p \nmid N$ , and character  $\varepsilon = \varepsilon_N \varepsilon_p$ , where  $\varepsilon_N$  has conductor prime to  $p$  and the conductor of  $\varepsilon_p$  is  $p^c$ . Let  $u = \min(\lfloor \frac{r}{2} \rfloor, r - c)$ .

**Theorem.** *In the notation of Proposition 4.1 of the article, if  $\chi$  is a Dirichlet character of conductor  $p^v$  with  $v > u$ , then  $f_\chi$  is new of level  $Np^{\max(2v, c+v)} > Np^r$ , unless  $v = c$  and  $\chi$  is of the form  $\varepsilon_p^{-1} \chi'$ , where  $\chi'$  has conductor dividing  $p^{c-1}$ .*

*In the latter case, the level of the newform  $f \otimes \chi$  corresponding to  $f_\chi$  is the same as that of  $f \otimes (\chi')^{-1}$ ; in particular, it is strictly greater than  $Np^r$  unless  $\chi'$  has conductor at most  $p^u$ .*

*Proof.* By Theorem 3.1(ii) of [1],  $f_\chi$  is new of level  $Np^{\max(2v, c+v)}$ , unless  $\chi' = \varepsilon_p \chi$  has conductor strictly less than  $p^{\max(c, v)}$ , which is only possible if  $c = v$ .

We note that if  $\chi' = \varepsilon_p \chi$ , then  $f \otimes \chi = (f \otimes (\chi')^{-1}) \otimes \nu^{-1}$ , where  $\nu = (\chi')^{-2} \varepsilon_p$  is the  $p$ -part of the nebentypus of  $f \otimes (\chi')^{-1}$ . Up to a scalar this is  $W_p(f \otimes (\chi')^{-1})$ , where  $W_p$  is the Atkin–Lehner operator at  $p$ . Hence  $f \otimes \chi$  and  $f \otimes (\chi')^{-1}$  have the same level at  $p$ , as claimed.  $\square$

It follows immediately that the infimum of the levels of the newforms  $f \otimes \chi$ , as  $\chi$  runs through the set of all Dirichlet characters of  $p$ -power conductor, is attained for some character of conductor at most  $p^u$ , although it will also be attained for some characters outside this range if  $u < c$ .

Hence in part (1) of both Proposition 4.2 and Proposition 4.4, “of  $p$ -power conductor” needs to be corrected to “of conductor dividing  $p^u$ ”, but the last sentence of each of these two propositions holds without modification and the algorithm described in §5 is still valid.

---

Received by the editor April 18, 2013.

2010 *Mathematics Subject Classification.* Primary 11F70; Secondary 11F11, 11Y99.

©2014 American Mathematical Society  
Reverts to public domain 28 years from publication

## REFERENCES

- [1] A. O. L. Atkin and Wen Ch'ing Winnie Li, *Twists of newforms and pseudo-eigenvalues of  $W$ -operators*, *Invent. Math.* **48** (1978), no. 3, 221–243, DOI 10.1007/BF01390245. MR508986 (80a:10040)
- [2] David Loeffler and Jared Weinstein, *On the computation of local components of a newform*, *Math. Comp.* **81** (2012), no. 278, 1179–1200, DOI 10.1090/S0025-5718-2011-02530-5. MR2869056 (2012k:11064)

MATHEMATICS INSTITUTE, UNIVERSITY OF WARWICK, COVENTRY CV4 7AL, UNITED KINGDOM  
*E-mail address:* `d.a.loeffler@warwick.ac.uk`

DEPARTMENT OF MATHEMATICS, BOSTON UNIVERSITY, BOSTON, MASSACHUSETTS 02215  
*E-mail address:* `jsweinst@math.bu.edu`