

## ERRATA TO “APPROXIMATION CLASSES FOR ADAPTIVE HIGHER ORDER FINITE ELEMENT APPROXIMATION”

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ABSTRACT. It has been brought to our attention that there is an error in the statement of Theorem 2.2 of our article *Approximation classes for adaptive higher order finite element approximation*, Math. Comp. 83 (2014), no. 289, pp. 2127–2160. We briefly explain how this error can be corrected.

The following small mistakes were found in [2] and the corresponding corrections should be introduced:

- Statement of Proposition 2.1 (page 2129); statement of Theorem 2.2 (page 2130): replace  $s + \alpha \leq r + \frac{1}{\tau_*}$  by  $s + \alpha < r + 1$ .
- Second line of Section 4.2 (page 2142), replace  $s < r + \max\{1, \frac{1}{p}\} = r + \frac{1}{p^*}$  by  $s < r + 1$ .
- Remark 4.8 (page 2143): Replace  $s < r' + \max\{1, \frac{1}{p}\}$  by  $s < r' + 1$ .
- Remark 4.9 (page 2144): Replace  $r > s - \max\{1, \frac{1}{p}\}$  by  $r > s - 1$ .
- Lemma 4.15 (page 2147): Replace  $s < r + \frac{1}{\tau_*}$  by  $s < r + 1$ .
- Lemma 4.17 (page 2148): Replace  $\alpha + s < r + \frac{1}{\tau_*}$  by  $\alpha + s < r + 1$ .

These mistakes come from the definition of Besov space at the beginning of Section 4.2 (page 2142). It is incorrect. It should be defined for  $s < r + 1$  instead of  $s < r + \max\{1, \frac{1}{p}\} = r + \frac{1}{p^*}$ . The wrong definition of Besov spaces comes from Remark 4.8, where we say

“The definition of  $B_{p,q}^s(\Omega)$  is independent of  $r$  in the sense that if  $r$  is replaced by  $r' \in \mathbb{N}$  with  $s < r' + \max\{1, \frac{1}{p}\}$ , then the resulting space is the same with equivalent (quasi)norms.”

This statement is incorrect. The correct one is with  $s < r' + 1$  instead of  $s < r' + \max\{1, \frac{1}{p}\}$ . The correct statement is proved in Theorem 10.1, page 55 of [1], making use of Marchaud’s inequality. It does not hold under the weaker assumption  $s < r' + \frac{1}{p}$  (when  $p < 1$ ). Marchaud’s inequality stated at the bottom of page 2143 is correct, and comes from Theorems 8.1–8.2, pages 47–48 of [1].

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