

be sufficient to establish that $\lim_{n \rightarrow \infty} f_n(x) = f_0(x)$ at every point x on $[0, p]$. The theorem follows immediately then from §5.1 and the fact that

$$f_n(x) = F_n^{-1} [[x]/p + F_n(x - [x])/p], 0 \leq x \leq p, n = 0, 1, \dots$$

Theorem 5 establishes the continuity of T from E_p onto E_p^* .

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THE NONLINEAR DIFFERENTIAL EQUATION

$$y'' + p(x)y + cy^3 = 0$$

EDMUND PINNEY¹

Among the limited number of nonlinear differential equations whose exact solutions are known is to be included

$$(1) \quad y''(x) + p(x)y(x) + c/y^3(x) = 0,$$

for c constant and $p(x)$ given. The general solution for which $y(x_0) = y_0 \neq 0$, $y'(x_0) = y'_0$ is

$$(2) \quad y(x) = [u^2(x) - cW^{-2}v^2(x)]^{1/2},$$

where u, v form a fundamental set of solutions of the linear equation

$$(3) \quad y''(x) + p(x)y(x) = 0$$

for which $u(x_0) = y_0$, $u'(x_0) = y'_0$, $v(x_0) = 0$, $v'(x_0) \neq 0$, where W is their Wronskian: $W = uv' - u'v = \text{const.} \neq 0$, and where the radical in (2) stands for that root which at x_0 has the value y_0 .

The proof is very simple and will be omitted.

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