

PROCEEDINGS
OF THE
AMERICAN MATHEMATICAL SOCIETY

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Bulletin of the American Mathematical Society

This journal is the official organ of the Society. It reports official acts of the Society and the details of its meetings. It contains some of the officially invited addresses presented before the Society, reviews of advanced mathematical books, research problems and a department of research announcements.

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This journal is devoted to abstracts and reviews of the current mathematical literature of the world. Two volumes will be published in 1963, Volume 25 and Volume 26. Each volume will consist of 6 regular issues plus an index issue. In each regular issue the abstracts and reviews are grouped under subject headings. Publication began in 1940.

Subscription price per volume of 7 issues is \$50.00; 2 volumes per year \$100.00. Back issues: volumes 1-16 (1940-1955) \$42.00 per volume; volumes 17-24 (1956-1962) \$50.00 per volume.

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This is a cover to cover translation into English of Acta Mathematica Sinica, published by Academia Sinica Peking, People's Republic of China. Acta Mathematica Sinica contains current research in all fields of pure mathematics. Two volumes, Vols. 2 and 3, are planned for 1963. Vol. 1 (1962) \$30.00. Subscription price per volume is \$20.00.

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