

ADDENDUM TO  
"A FIXED POINT THEOREM FOR HYPERSPACES  
OF  $\lambda$  CONNECTED CONTINUA"

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When defining  $f^*$  in lines 13–15 on p. 232 of [1], we must assume that the complementary domain  $U$  of  $f[\text{Bd } B]$  that contains  $f[D_4]$  is unbounded. Hence it may be necessary to adjust the position of  $f[D]$  in  $E^2$ . The adjustment must be made without changing the way  $f[\text{Bd } D']$  separates  $f[D]$  in  $E^2$ . This can be accomplished by moving the point at infinity in the one-point compactification of  $E^2$  to a point of  $U - f[D]$ . The following argument shows that  $U - f[D]$  is not empty.

Let

$$V = \{(x, y) | x = 6 \text{ and } 0 < y < 6\},$$

$$Q_1 = \{(x, y) | 11/2 \leq x \leq 6 \text{ and } 0 < y < 6\}, \text{ and}$$

$$Q_2 = \{(x, y) | 5 < x \leq 11/2 \text{ and } 0 < y < 6\}.$$

Assume  $U$  is a subset of  $f[D]$ . It follows that  $f[Q_2]$  separates  $f[V]$  from  $f[\text{Bd } B]$  in  $E^2$ . To see this assume the contrary. Let  $A$  be an arc in the closure of  $U$  that goes from  $f[V]$  to  $f[\text{Bd } B]$  and misses  $f[Q_2]$ . Since  $f$  is a  $\frac{1}{2}$ -map,  $f[Q_1]$  and  $f[\text{Bd } B]$  are disjoint. Hence  $f[Q_1]$  does not contain  $A$ . Let  $z$  be the last point of  $A$  that belongs to  $f[Q_1]$ . Since  $A$  is in  $f[D] - f[Q_2]$ , every point of  $A$  that follows  $z$  is in  $f[D_2 - B]$ . Hence  $z$  belongs to  $f[D_2 - B]$ , which contradicts the fact that  $f$  is a  $\frac{1}{2}$ -map. Therefore  $f[Q_2]$  separates  $f[V]$  from  $f[\text{Bd } B]$  in  $E^2$ .

For  $i = 1, 2$ , and  $3$ , let  $T_i = \{(x, y) | 5 < x \leq 11/2 \text{ and } 2i - 2 < y < 2i\}$ . The continuum  $f[Q_2]$  is the union of  $H = f[T_1] \cup f[T_2]$  and  $K = f[T_2] \cup f[T_3]$ . Furthermore,  $H \cap K$  is the continuum  $f[T_2]$ . It follows from Janiszewski's theorem [3, Theorem 20, p. 173] that either  $H$  or  $K$  separates  $f[V]$  from  $f[\text{Bd } B]$  in  $E^2$ .

Assume without loss of generality that  $H$  separates  $f[V]$  from  $f[\text{Bd } B]$  in  $E^2$ . Let  $W = \{(x, y) | 1 < x \leq 6 \text{ and } y = 5\}$ . The continuum  $f[W]$  meets both  $f[V]$  and  $f[\text{Bd } B]$ . Since  $f$  is a  $\frac{1}{2}$ -map,  $f[W]$  misses  $H$ . This contradicts the

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Received by the editors July 23, 1976.

AMS (MOS) subject classifications (1970). Primary 54B20, 54C10, 54F20, 54F60, 54H25; Secondary 54C05, 54F25, 54F55.

*Key words and phrases.* Hyperspace, chainable continua, arc-like continua, circle-like continua, fixed point property, lambda connectivity, hereditarily decomposable continua, disk-like continua, triod, snake-like continua, unicoherence,  $\epsilon$ -map into the plane, antipodal points, Borsuk-Ulam theorem.

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assumption that  $H$  separates  $f[V]$  from  $f[\text{Bd } B]$  in  $E^2$ . It follows that  $f[D]$  does not contain  $U$ .

The theorem referred to in the last sentence in the proof of Theorem 2 of [1] should be compared with an earlier theorem of W. T. Ingram [2, Theorem 5].

In the second sentence in the proof of Theorem 3 of [1], we should also refer to J. T. Rogers' theorem [4, Proposition 2.2].

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