

This result and (14) then imply

$$\sigma^2 = \frac{1}{4} \int_0^\infty [M(\omega)M(-\omega) + M(\omega)\{M(\omega)\}_c + \{M(-\omega)\}_c M(-\omega) + \{M(-\omega)M(\omega)\}_c] w_x(f) df, \quad (15)$$

which immediately reduces to (4).

If in place of equation (7) we start with

$$\psi_z(t; \tau) = \mathcal{E}z(t)z(t + \tau)$$

and employ the Wiener-Khintchine relations<sup>1</sup> to write

$$w_z(t; f) = 2 \int_{-\infty}^\infty \psi_z(t; \tau) e^{-i\omega\tau} d\tau$$

as the time dependent spectral density, then using the above techniques we can show that

$$w_z(t; f) = \frac{1}{4} H(j\omega) \left\{ \sum_{m=1}^N a_m [\{M(\omega - \omega_m)\}_c + M(-\omega + \omega_m)] e^{i(\omega_m t + \phi_m)} w_x(f - f_m) + \sum_{m=1}^N a_m [\{M(\omega + \omega_m)\}_c + M(-\omega - \omega_m)] e^{-i(\omega_m t + \phi_m)} w_x(f + f_m) \right\}. \quad (16)$$

It is easily seen, then, that

$$\sigma^2 = \frac{1}{2} \int_{-\infty}^\infty w_z(t; f) df$$

where  $\sigma^2$  is given by (4).

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<sup>1</sup>D. G. Lampard, *Generalization of the Wiener-Khintchine theorem to nonstationary processes*, J. Appl. Phys. 25, 802-803(1954)

### Correction to the paper

#### DUALITY IN NONLINEAR PROGRAMMING

Quarterly of Applied Mathematics, XX, 300-302 (1962)

By O. L. MANGASARIAN (*Shell Development Company*)

There is an incorrect statement of a previous result. In particular the last sentence of the Converse Duality Theorem should read:

"If  $\varphi(x)$  is quadratic and if  $g(x)$  is linear, then a weaker converse theorem is also true if  $\varphi(x)$  is merely convex and twice continuously differentiable."