# St. Petersburg Mathematical Journal

(Formerly Leningrad Mathematical Journal)

Volume 23 Number 2 April 2012

A Translation of

РОССИЙСКАЯ АКАДЕМИЯ НАУК

АЛГЕБРА И АНАЛИЗ ТОМ 23 № 2 2011



American Mathematical Society

Providence, Rhode Island USA ISSN 1061-0022

#### ST. PETERSBURG MATHEMATICAL JOURNAL

(Formerly Leningrad Mathematical Journal) A translation of the Russian bimonthly Алгебра и анализ

"Наука", С.-Петербургское отделение, 2011 г.

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The Editorial Board cordially congratulates Editor-in-Chief Sergei Vital'evich Kislyakov

on the occasion of his birthday. We wish him health and every success in his research and in his guidance of our journal.



**Viktor Abramovich Zalgaller** turned 90 on December 25, 2010.

Dear Viktor Abramovich,

We congratulate you—remarkable man, mathematician, and writer—on the occasion of your milestone birthday anniversary and wish you to enjoy sound health, unfading good spirits, and happiness to be with your loving family and friends.

Editorial Board

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 $<sup>^*</sup>$ The American Mathematical Society scheme for transliteration of Cyrillic may be found at the end of index issues of *Mathematical Reviews*.

