

# St. Petersburg Mathematical Journal

(Formerly Leningrad Mathematical Journal)

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Volume 30 Number 3 June 2019

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*A Translation of*

РОССИЙСКАЯ АКАДЕМИЯ НАУК

АЛГЕБРА  
И  
АНАЛИЗ

ТОМ 30 № 3 2018



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# ST. PETERSBURG MATHEMATICAL JOURNAL

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*A translation of the Russian bimonthly*

Алгебра и анализ

“Наука”, С.-Петербургское отделение, 2018 г.

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This issue is dedicated to the memory of Mikhail Zakharovich Solomyak,  
our friend, teacher, and colleague.  
—The editors and authors



Mikhail Zakharovich Solomyak  
(May 16, 1931–July 31, 2016)

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