

# St. Petersburg Mathematical Journal

(Formerly Leningrad Mathematical Journal)

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Volume 33 Number 1 February 2022

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*A Translation of*

РОССИЙСКАЯ АКАДЕМИЯ НАУК

АЛГЕБРА

И

АНАЛИЗ

ТОМ 33 № 1 2021



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# ST. PETERSBURG MATHEMATICAL JOURNAL

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*A translation of the Russian bimonthly*

Алгебра и анализ

“Наука”, С.-Петербургское отделение, 2021 г.

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## CONTENTS

### Research Papers

<b>D. V. Artamonov</b> , Clebsh–Gordan coefficients for the algebra $\mathfrak{gl}_3$ and hypergeometric functions .....	1
<b>Yu. S. Belousov, M. V. Karev, A. V. Malyutin, A. Yu. Miller, and E. A. Fominykh</b> , Lernaean knots and band surgery .....	23
<b>S. V. Buyalo</b> , Symmetries of double ratios and an equation for Möbius structures .....	47
<b>S. V. Ivanov</b> , Distance difference functions on nonconvex boundaries of Riemannian manifolds .....	57
<b>M. Lanini and K. Zainoulline</b> , Twisted quadratic foldings of root systems ...	65
<b>B. M. Makarov and A. N. Podkorytov</b> , On the sharpness of assumptions in the Federer theorem .....	85
<b>I. Panin and C. Walter</b> , Quaternionic Grassmannians and Borel classes in algebraic geometry .....	97
<b>N. S. Ustinov</b> , Solvability of a critical semilinear problem with the spectral Neumann fractional Laplacian .....	141
<b>N. D. Filonov</b> , Schrödinger operator with decreasing potential in a cylinder ...	155
<b>R. Hazrat and Huanhuan Li</b> , A note on the centralizer of a subalgebra of the Steinberg algebra .....	179

## RUSSIAN CONTENTS\*

### СОДЕРЖАНИЕ

#### Статьи

<i>Артамонов Д. В.</i> Коэффициенты Клебша–Гордана для $\mathfrak{gl}_3$ и гипергеометрические функции . . . . .	1
<i>Белоусов Ю. С., Карев М. В., Малютин А. В., Миллер А. Ю., Фоминых Е. А.</i> Лернейские узлы и вложенные перестройки . . . . .	30
<i>Буяло С. В.</i> Симметрии двойных отношений и уравнение для мёбиусовых структур . . . . .	67
<i>Иванов С. В.</i> Разностно-дистанционные функции на невыпуклых краях римановых многообразий . . . . .	81
<i>Lanini M., Zainoulline K.</i> Twisted quadratic foldings of root systems . . . . .	93
<i>Макаров Б. М., Подкорытов А. Н.</i> О точности условий теоремы Федерера . . . . .	119
<i>Panin I., Walter C.</i> Quaternionic Grassmannians and Borel classes in algebraic geometry . . . . .	136
<i>Устинов Н. С.</i> О разрешимости полулинейной задачи со спектральным дробным лапласианом Неймана и критической правой частью . . . . .	194
<i>Филонов Н. Д.</i> Оператор Шрёдингера в цилиндре с убывающим потенциалом . . . . .	213
<i>Hazrat R., Huanhuan Li</i> A note on the centralizer of a subalgebra of the Steinberg algebra . . . . .	246

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