

Theory of Probability and Mathematical Statistics

Number 79 2009

A Translation of

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ЙМОВІРНОСТЕЙ ТА
МАТЕМАТИЧНА
СТАТИСТИКА

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