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Number 83 2011

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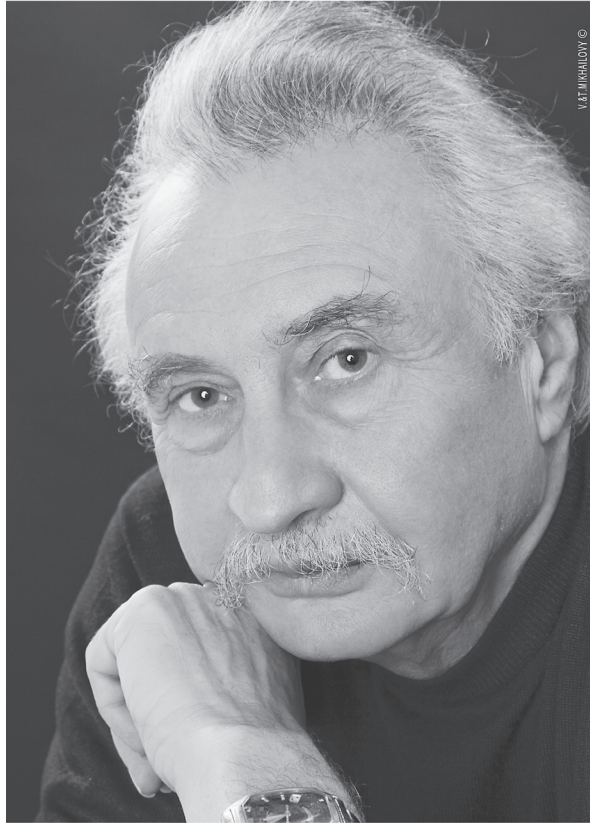
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The members of the Department of Probability Theory, Statistics, and Actuarial Mathematics of the Faculty for Mechanics and Mathematics of Kyiv National Taras Shevchenko University, and the Editorial Board of the journal *Theory of Probability and Mathematical Statistics* congratulate Deputy Editor-in-Chief of the journal, winner of the State Prize of Ukraine in Science and Technology, Honored Scientist of Ukraine, Professor **Yuriï Vasyl'ovich Kozachenko** on the occasion of his 70th birthday and wish him robust health and creative longevity.

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<i>С. В. Шкляр</i>	
Умови конзистентності оцінки найменших квадратів у всіх змінних у моделі векторної лінійної регресії з похибками в змінних	148
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