# Mathematical Tables 

and other
Aids to Computation

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A. Arithmetical Tables. Mathematical Constants
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H. Numerical Solution of Equations
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L. Higher Mathematical Functions
M. Integrals

N . Interest and Investment
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Q. Astronomy
R. Geodesy
S. Physics, Geophysics, Crystallography
T. Chemistry
U. Navigation
V. Aerodynamics, Hydrodynamics, Ballistics
Z. Calculating Machines and Mechanical Computation

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