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Mathematics of Computation

TABLE OF CONTENTS

OCTOBER 1973

Generalized Local Maximum Principles for Finite-Difference Operators ACHI BRANDT	685
Convergence for a Vortex Method for Solving Euler's Equation THEODORE E. DUSHANE	719
Symmetrization of the Fluid Dynamic Matrices with Applications ELI TURKEL	729
Stability and Convergence of Difference Approximations to Pseudo-Parabolic Partial Differential Equations WILLIAM H. FORD & T. W. TING	737
Mesh Refinements for Parabolic Equations of Second Order Stewart Venit	745
Eigenfrequencies of an Elliptic Membrane B. A. TROESCH & H. R. TROESCH	755
Elliptical Membranes with Smallest Second Eigenvalue B. Andreas Troesch	767
A Posteriori Error Bounds for Numerical Solutions of the Neutron Transport Equation	773
A Modified Bairstow Method for Multiple Zeros of a Polynomial F. M. CARRANO	781
The Order of Numerical Methods for Ordinary Differential Equations J. C. BUTCHER	793
Approximate Solution of the Differential Equation $y'' = f(x, y)$ with Spline Functions	807
Polynomial Approximation of a Function and Its First Derivative in Near Minimax Norms Edgar A. Cohen, Jr.	817
Boundary Expansions for Spline Interpolation W. D. HOSKINS	829
Integration Formulas and Schemes Based on g-Splines George D. Andria, George D. Byrne & David R. Hill	831
An Elliptic Integral Identity H. S. WRIGGE	839
Rational Approximants Defined from Double Power Series J. S. R. CHISHOLM	841
Error Analysis for Direct Linear Integral Equation Methods JAMES L. PHILLIPS	849
Numerical Construction of Gaussian Quadrature Formulas for	
$\int_0^1 (-\text{Log } x) \cdot x^{\alpha} \cdot f(x) \cdot dx$ and $\int_0^{\infty} E_m(x) \cdot f(x) \cdot dx$. Bernard Danloy	861
A Note on the Computation of Integrals Involving Products of Trigonometric and Bessel Functions Peter Linz & T. E. Kropp	871
Self-Scaling Variable Metric Algorithms Without Line Search for Unconstrained Minimization SHMUEL S. OREN	873
An Algorithm for the Exact Reduction of a Matrix to Frobenius Form Using Modular Arithmetic. I Jo Ann Howell	887
An Algorithm for the Exact Reduction of a Matrix to Frobenius Form Using Modular Arithmetic. II Jo Ann Howell	905
An Extrapolated Gauss-Seidel Iteration for Hessenberg Matrices L. J. LARDY	921
Extensions of Forsythe's Method for Random Sampling from the Normal Distribution J. H. Ahrens & U. Dieter	927

New Approximations to Familiar Functions	
J. E. DUTT, T. K. LIN & L. C. TAO	939
A Search Procedure and Lower Bound for Odd Perfect Numbers BRYANT TUCKERMAN	943
A Lower Bound for the Set of Odd Perfect Numbers Peter Hagis, Jr. On the Largest Prime Divisor of an Odd Perfect Number	951
PETER HAGIS, JR. & WAYNE L. McDANIEL	955
The First Occurrence of Large Gaps Between Successive Primes RICHARD P. BRENT	959
Computational Problems in S-Function Theory P. A. MORRIS	965
A Note on Dirichlet Characters RICHARD H. HUDSON	973
Primitive Binary Polynomials Wayne Stahnke	977
The Determination of Galois Groups RICHARD STAUDUHAR	981
REVIEWS AND DESCRIPTIONS OF TABLES AND BOOKS	997
Bulington 43, Cherkasova 45, Day 55, Fettis, Caslin & Cramer 49, Fettis & Caslin 50, Hagis 53, Jacoby, Kowalik & Pizzo 46, Karmazina 48, Morris 54, Robinson 44, Schatz 42, Tuckerman 51, Tuckerman 52, Young 47.	
TABLE ERRATA	1009
CORRIGENDA CHORIN, TE RIELE, SHANKS & SERAFIN	1011
MICROFICHE SUPPLEMENT Integration Formulas and Schemes Based on g-Splines GEORGE D. Andria, George D. Byrne & David R. Hill	
Indices to Volume XXVII	1013

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Volume 5, 480 pages, June 1974:

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Algebraic number theory—local and p-adic fields;

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Volume 6, 424 pages, February 1974:

General;

Subject index;

Author index.

Orders are now being accepted for these three sets of review volumes. It should be noted that the two collections on group theory can be purchased as a set, and that the number theory volumes may be purchased individually, although it is suggested that those purchasing single volumes of the number theory set also purchase Volume 6 which contains the indexes.

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Computational Problems in S-Function Theory P. A. Morris	965
A Note on Dirichlet Characters RICHARD H. HUDSON	973
Primitive Binary Polynomials WAYNE STAHNKE	977
The Determination of Galois Groups RICHARD STAUDUHAR	981
REVIEWS AND DESCRIPTIONS OF TABLES AND BOOKS	997
Bulington 43, Cherkasova 45, Day 55, Fettis, Caslin & Cramer 49, Fettis & Caslin 50, Hagis 53, Jacoby, Kowalik & Pizzo 46, Karmazina 48, Morris 54, Robinson 44, Schatz 42, Tuckerman 51, Tuckerman 52, Young 47.	
Table Errata	1009
Corrigenda	1011
MICROFICHE SUPPLEMENT Integration Formulas and Schemes Based on g-Splines GEORGE D. ANDRIA, GEORGE D. BYRNE & DAVID R. HILL	
INDICES TO VOLUME XXVII	1013

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TABLE OF CONTENTS

OCTOBER 1973

Generalized Local Maximum Principles for Finite-Difference Operators ACHI BRANDT	685
Convergence for a Vortex Method for Solving Euler's Equation THEODORE E. DUSHANE	719
Symmetrization of the Fluid Dynamic Matrices with Applications ELI TURKEL	729
Stability and Convergence of Difference Approximations to Pseudo-Parabolic	
Partial Differential Equations WILLIAM H. FORD & T. W. TING Mesh Refinements for Parabolic Equations of Second Order	737
STEWART VENIT Eigenfrequencies of an Elliptic Membrane	745
B. A. TROESCH & H. R. TROESCH Elliptical Membranes with Smallest Second Eigenvalue	755
B. ANDREAS TROESCH A Posteriori Error Bounds for Numerical Solutions of the Neutron Transport	767
Equation NIEL K. MADSEN	773
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An Algorithm for the Exact Reduction of a Matrix to Frobenius Form Using Modular Arithmetic. I Jo Ann Howell	887
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An Extrapolated Gauss-Seidel Iteration for Hessenberg Matrices L. J. LARDY	921
Extensions of Forsythe's Method for Random Sampling from the Normal	
Distribution J. H. Ahrens & U. Dieter	927