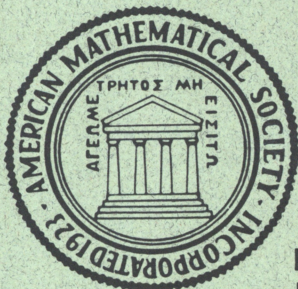


Mathematics of Computation



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all material submitted to

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should be sent to

Professor Walter Gautschi
Computer Sciences Department
Purdue University
West Lafayette, IN 47907

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