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Roger D. Nussbaum and Heinz-Otto Peitgen

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Fluid Dynamics in Astrophysics and Geophysics Norman R. Lebovitz, Editor

LECTURES IN APPLIED MATHEMATICS, VOLUME 20

This book features two main articles on geophysical fluid dynamics and on astrophysical fluid dynamics (by Rhines and Schutz, respectively), some timely articles on currently interesting topics in these areas, and a couple of articles on mathematical methods which are finding applications in these two areas of science.

The hope is that the juxtaposition of these two fields of application of fluid dynamics will help to expose their common foundations and methods, and open up their problem areas to a wider scientific community.

Applied mathematicians interested in acquiring a background in astro- or geophysics, and who want to understand the areas common to these two disciplines, will find these papers illuminating.

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Large-Scale Computations in Fluid Mechanics Bjorn E. Engquist, Stanley Osher and Richard C. J. Somerville, Editors

This is the proceedings of an AMS-SIAM Summer Seminar on Applied Mathematics held at Scripps Institution of Oceanography in 1983, whose purpose was to bring scientists interested in computational fluid mechanics together with numerical analysts and mathematicians working in large-scale computations. The complexity of many contemporary problems of fluid mechanics is so great as to tax the capabilities of present-day computers. There is a real need and opportunity for numerical analysis to aid research on the physical problems of achieving optimal utilization of current computers.

Fifty lectures were given on subjects equally divided between mathematics and applications. The numerical modeling included geophysical problems of the atmosphere, ocean, and interior of the earth, and planetary, solar, and stellar atmospheres. Applications ranged from idealized turbulence in laboratory convection models to operational weather prediction. Engineering applications included aerodynamics, combustion, and flow in porous media. Recent advances in numerical analysis which have applications to these problems were stressed. These include shock capturing algorithms, spectral methods, boundary treatments, vortex methods, and parallel computing.

In addition to specialized research lectures, several speakers gave talks surveying important areas of numerical analysis and computational fluid dynamics.

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