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C. Anthony Hester* (anthonyhester@davidson-tech.com). *Semigroups Generated by Pseudo-contractive Mappings Under the Nagumo Condition.*

Let C be a closed subset of a Banach space X whose topological dual space X^* is uniformly convex. Using strong measurability, the Pettis integral, the weak derivative, and other concepts from the calculus of vector-valued functions, one may show that, for any demicontinuous weakly Nagumo k -pseudo-contractive mapping $T : C \rightarrow X$, $A = T - I$ weakly generates a semigroup of type $k - 1$ on C . If $k < 1$ (id est, if T is strongly pseudo-contractive), then the semigroup consists of contraction operators. A family of commuting contraction operators on C necessarily has a unique common fixed point, consequently, T has a unique fixed point. This implies that, if T is pseudo-contractive ($k = 1$) and C is also bounded and convex, then T has at least one fixed point. But T is weakly inward when C is convex and self-mappings are always weakly inward, hence, any demicontinuous pseudo-contractive mapping $T : C \rightarrow C$ has a fixed point when C is closed, bounded, and convex. This answers an important question in fixed point theory which has been open for quite some time. (Received August 12, 2008)