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**Joel Avrin\*** (jdavrin@uncg.edu), Department of Mathematics and Statistics, University of North Carolina at Charlotte, 9201 University City Blvd, Charlotte, NC 28223-0001. *Attractor and inertial-manifold results for the 3-D spectrally-hyperviscous Navier-Stokes equations.*

Let  $P_m$  project onto the first  $m$  eigenmodes of  $A = -\Delta$ , and let  $Q_m = I - P_m$ , then we add to the 3-D incompressible Navier-Stokes equations the term  $\mu A_\varphi u$  where the operator  $A_\varphi$  satisfies  $A_\varphi \geq Q_m A^\alpha$  ( $\alpha \geq 2$ ) in the sense of quadratic forms. A distinguished class of  $A_\varphi$  is zero on the first  $m_0$  eigenmodes for  $m_0 \leq m$ . We obtain global regularity and a compact global attractor  $\mathcal{A}$  with Hausdorff and fractal dimensions bounded by  $Km^a\kappa^b$  where  $\kappa$  is the Kolmogorov wavenumber,  $K$  is generally within an order of magnitude of unity,  $a$  is a fractional power, and  $b < 3$ . In particular  $m^a\kappa^b \leq \kappa^3$  for  $m \leq \kappa^3$ , i.e. for  $m$  so large as to suggest machine-indistinguishability from NSE solutions. This robust conformance with the Landau-Lifschitz estimates appears to be unique among NSE closure models, and  $b$  is significantly lower for more realistic choices of  $m$ . We also obtain the existence of inertial manifolds which imply in the distinguished-class case that for  $m$  large enough eigenmodes free of hyperviscosity control the essential dynamics. (Received February 28, 2009)