

1054-16-104

Arkady Berenstein* (arkadiy@math.uoregon.edu), 4936 Mahalo Drive, Eugene, OR 97405,
and **Vladimir Retakh** (vretakh@math.rutgers.edu), 110 Frelinghuysen Road, Piscataway, NJ
08854-8019. *Lie algebras and Lie groups over noncommutative rings.*

In my talk I will introduce a version of Lie algebras and Lie groups over noncommutative rings.

For any Lie sub-algebra \mathfrak{g} of an associative algebra A and any associative ring F , I will define a Lie algebra $(\mathfrak{g}, A)(F)$ functorially in F and A . In particular, if F is commutative, the Lie algebra $(\mathfrak{g}, A)(F)$ is simply the loop Lie algebra of \mathfrak{g} with coefficients in F .

In the case when \mathfrak{g} is semisimple or Kac-Moody, I will explicitly compute $(\mathfrak{g}, A)(F)$ in terms of commutator ideals of F (surprisingly, these ideals have previously emerged as building blocks in M. Kapranov's approach to noncommutative geometry).

To each Lie algebra $(\mathfrak{g}, A)(F)$ one associates a "noncommutative algebraic" group of automorphisms. I will conclude my talk with examples of such groups and with the description of "noncommutative root systems" of rank 1. (Received September 15, 2009)