1010-93-108

Irina F. Sivergina* (isivergi@kettering.edu), Department of Science and Mathematics, 1700 Third West Avenue, Flint, MN 48504, and Michael P. Polis (polis@oakland.edu). A Null Controllability of a Quasi-Static Thermoelastic Plate. Preliminary report.

We study the null controllability of the system

$$\begin{cases} (1+a^2)\theta_t = \Delta\theta + a\frac{d}{dt} \max\{a \int_{\Omega} \theta(x,t) \, dx - g, \, 0\} + v(x,t), \\ x \in \Omega \subset R^n, \ t > 0 \\ \theta(x,0) = \theta_0(x), \text{ in } \Omega \\ \theta(x,t) = 0, \text{ in } \Gamma_d \times (0,T) \\ \frac{\partial \theta(x,t)}{\partial \nu} = k(a \int_{\Omega} \theta(x,t) \, dx - g) \theta(x,t), \text{ in } \Gamma_c \times (0,T). \end{cases}$$
(1)

Here Ω is an open bounded domain in \mathbb{R}^n with a piece-wise smooth boundary $\Gamma = \Gamma_d \cup \Gamma_c$, $k(s), s \in \mathbb{R}$, is a scalar nonnegative differentiable function, and v(x,t) is regarded as a control.

Theorem. For any $\theta_0 \in H^1(\Omega)$, $\theta_0(x) = 0$ for $x \in \Gamma_d$, there is a control $v \in L^2(\Omega_T)$, $\Omega_T = \Omega \times (0, T)$, such that there exists a unique solution $\theta \in W^{2,1}(\Omega_T)$ to (1) and $\theta(\cdot, T) = 0$. Further, for any $\theta_0 \in L^2(\Omega)$ and any $\epsilon > 0$, there is a control $v \in L^2(\Omega_T)$, such that $\|\theta(\cdot, T)\| < \epsilon$. (Received August 22, 2005)