## 1011-53-218 Jeanne N. Clelland\*, Department of Mathematics, 395 UCB, University of Colorado, Boulder, CO 80309-0395, and Christopher G. Moseley and George R. Wilkens. Geometry of sub-Finsler Engel manifolds.

A sub-Riemannian Engel manifold consists of a 4-manifold X, a 2-plane field  $D \subset TX$  with the property that [D, D] has rank 3 everywhere and [D, [D, D]] = TX, and a Riemannian metric on each 2-plane D. Many aspects of the geometry of sub-Riemannian Engel manifolds have been described by C. Moseley. In this talk, we introduce the notion of a sub-Finsler Engel manifold, in which the Riemannian metric on each 2-plane D is replaced by a Finsler metric. We will explain why this is a natural generalization from the point of view of control theory, discuss how the geometry differs from the sub-Riemannian case, and consider examples. (Received August 27, 2005)