

PROCEEDINGS
OF THE
AMERICAN MATHEMATICAL SOCIETY

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RICHARD BRAUER SHIZUO KAKUTANI
A. C. SCHAEFFER

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