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NOTE ON A PAPER OF CIVIN AND YOOD

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It is possible to obtain stronger results than those of [1] in a small amount of space through the use of a different method. We follow the notation of [1] throughout.

THEOREM 1. Let B be a complex commutative B anach algebra with countable space \mathfrak{M} of maximal regular ideals. Let A be a separating subalgebra. Then (i) if A is not contained in any maximal regular ideal it is determining. Otherwise (ii) there exists a (unique) maximal regular ideal M of B with \hat{A} dense in \hat{M} .

PROOF. If $x \in A$ then $\operatorname{Cl}[\hat{x}(\mathfrak{M})] = \hat{x}(\mathfrak{M}) \cup \{0\}$ is a countable compact set. Then by a theorem of Lavrent'ev [2], polynomials in z are uniformly dense on $\operatorname{Cl}[\hat{x}(\mathfrak{M})]$ in all continuous complex valued functions on $\operatorname{Cl}[\hat{x}(\mathfrak{M})]$ and in particular uniformly approximate \bar{z} on $\operatorname{Cl}[\hat{x}(\mathfrak{M})]$, i.e. polynomials in \hat{x} uniformly approximate \hat{x}^- on \mathfrak{M} . Then, $\operatorname{Cl}[\hat{A}]$ being a uniformly closed, separating, self adjoint algebra of continuous, complex valued functions vanishing at ∞ on a locally compact space \mathfrak{M} , equals $\mathfrak{C}(\mathfrak{M})$ in case (i) or at worst some unique $\operatorname{Cl}[\widehat{\mathfrak{M}}]$ in case (ii) by the Stone-Weierstrass approximation theorem [3].

Theorem 3.3 and extensions of Theorem 3.5 and Corollary 3.6 of [1] eliminating the hypothesis of regularity and the necessity of limiting the discussion to maximal subalgebras follow as simple corollaries, e.g.

COROLLARY 2. The only closed separating subalgebras of a complex commutative B^* -algebra with a countable space of maximal regular ideals are these maximal regular ideals themselves.

The method of proof of Theorem 1 and the Lavrent'ev Theorem will also yield the following more general version:

THEOREM 3. If A is a separating subalgebra of a complex commutative Banach algebra B such that all $x \in A$ have spectrum plus $\{0\}$ nowhere dense, nonseparating sets of complex numbers, then A is determining if it is not contained in a maximal regular ideal, and otherwise \hat{A} is dense in \hat{M} for some unique maximal regular ideal M of B.

A number of related results are readily derivable from this theorem.

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