

PROCEEDINGS
OF THE
AMERICAN MATHEMATICAL SOCIETY

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VOLUME 14, NUMBER 5
OCTOBER, 1963

PUBLISHED BY THE AMERICAN MATHEMATICAL SOCIETY
PROVIDENCE, RHODE ISLAND

Journals Published by the American Mathematical Society

Bulletin of the American Mathematical Society

This journal is the official organ of the Society. It reports official acts of the Society and the details of its meetings. It contains some of the officially invited addresses presented before the Society, reviews of advanced mathematical books, research problems and a department of research announcements.

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Second-class postage paid at Providence, Rhode Island and additional mailing offices. Authorization is granted under the authority of the act of August 24, 1912, as amended by the act of August 4, 1947 (sec. 34.21, P. L. & R.). Acceptance for mailing at the special rate of postage provided for in section 34.40, paragraph d., P. L. & R.

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Printed in the United States of America

Journals Published by the American Mathematical Society

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This journal is devoted to abstracts and reviews of the current mathematical literature of the world. Two volumes will be published in 1963, Volume 25 and Volume 26. Each volume will consist of 6 regular issues plus an index issue. In each regular issue the abstracts and reviews are grouped under subject headings. Publication began in 1940.

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Current subscriptions are as follows: Domestic, \$17.50; foreign, \$20.00. Single issues are \$5.00. Volumes 1, 2, 3, and 4 (1960-1963) are available at \$30.00 per volume or \$5.00 per issue.

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This is a cover to cover translation into English of *Acta Mathematica Sinica*, published by Academia Sinica Peking, People's Republic of China. *Acta Mathematica Sinica* contains current research in all fields of pure mathematics. Two volumes, Vols. 2 and 3, are planned for 1963. Vol. 1 (1962) \$30.00. Subscription price per volume is \$20.00.

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A journal devoted to original papers in numerical analysis, the application of numerical methods and high-speed calculator devices, the computation of mathematical tables, the theory of high-speed calculating devices and other aids to computation. In addition it publishes reviews and notes in these and related fields. Published by the Society for the National Academy of Sciences-National Research Council.

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