

PROCEEDINGS  
OF THE  
AMERICAN MATHEMATICAL SOCIETY

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## Journals Published by the American Mathematical Society

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### Bulletin of the American Mathematical Society

This journal is the official organ of the Society. It reports official acts of the Society and the details of its meetings. It contains some of the officially invited addresses presented before the Society, reviews of advanced mathematical books, research problems and a department of research announcements.

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### Mathematical Reviews

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