

PROCEEDINGS
OF THE
AMERICAN MATHEMATICAL SOCIETY

EDITED BY

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VOLUME 16, NUMBER 1
FEBRUARY, 1965

PUBLISHED BY THE AMERICAN MATHEMATICAL SOCIETY
PROVIDENCE, RHODE ISLAND

Journals Published by the American Mathematical Society

Bulletin of the American Mathematical Society

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Second-class postage paid at Providence, Rhode Island and additional mailing offices. Authorization is granted under the authority of the act of August 24, 1912, as amended by the act of August 4, 1947 (sec. 34.21, P. L. & R.). Acceptance for mailing at the special rate of postage provided for in section 34.40, paragraph d., P. L. & R.

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Printed in the United States of America

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GEORGE BANTA COMPANY, INC., MENASHA, WISCONSIN

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This journal is devoted to abstracts and reviews of the current mathematical literature of the world. Two volumes will be published in 1965, Volume 29 and Volume 30. Each volume will consist of 6 regular issues plus an index issue. In each regular issue the abstracts and reviews are grouped under subject headings. Publication began in 1940.

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